

**Figure 1.** Top:  $(u, v)$  coverage of the four M87 observing days in the 2017 campaign. The color of the data points codes the fractional polarization amplitude  $|\tilde{m}(u, v)|$  in the range from 0 to 2. Error bars on  $|\tilde{m}|$  are omitted for clarity. A few data points with very high fractional polarization  $|\tilde{m}(u, v)| \sim 2$  correspond to  $(u, v)$  points where the Stokes  $\mathcal{I}$  visibility amplitude profile has deep minima (SMA–SMT baselines). The data shown are derived from low-band visibilities after the initial calibration pipeline described in Section 3.2 but before any D-term calibration. The data points are coherently scanned-averaged. Bottom: M87 field rotation angle  $\phi$  for each station as a function of time.

Producing an image of the linearly polarized emission requires both solving for the distribution of Stokes parameters  $\mathcal{Q}$  and  $\mathcal{U}$  on the sky and for the complex D-terms that mix right and left circular polarization at the stations. In this work, we use several distinct methods to accomplish these tasks. Our approaches can be classified into three main categories: imaging via sub-component fitting; imaging via regularized maximum likelihood; and imaging as posterior exploration. In this section we only briefly describe each method: fuller descriptions are presented in Appendix C.

The calibration of the instrumental polarization by sub-component fitting has been performed using three different codes (LPCAL, GPCAL, and `polsolve`) that depend on two standard software packages for interferometric data analysis: AIPS<sup>3</sup> and CASA<sup>4</sup>. In all of these methods, the Stokes  $\mathcal{I}$  imaging step is performed using the CLEAN algorithm (Högbom 1974), and sub-components with constant complex fractional polarization are constructed from collections of the total intensity CLEAN components and fit to the data. In AIPS, two algorithms for D-term calibration are available: LPCAL (extensively used in VLBI polarimetry for

more than 20 years; Leppänen et al. 1995) and GPCAL<sup>5</sup> (Park et al. 2021). In CASA, we use the `polsolve` algorithm (Martí-Vidal et al., *in prep.*), which uses multiple calibrators simultaneously to fit polarimetric sub-components and allows for frequency-dependent D-terms (see Appendix D). In sub-component fitting and imaging with LPCAL and `polsolve` we assume that Stokes  $\mathcal{V} = 0$ . Further details on LPCAL, GPCAL, and `polsolve` can be found in Appendix C.1.

Image reconstruction via the Regularized Maximum Likelihood (RML) method was used in Paper IV along with CLEAN to produce the first total intensity images of the 230 GHz core in M87. RML algorithms find an image that maximizes an objective function composed of a likelihood term comparing the image to data, and regularizer terms that penalize or favor certain image features. In this work, we use the RML method implemented in the `eht-imaging`<sup>6</sup> software library (Chael

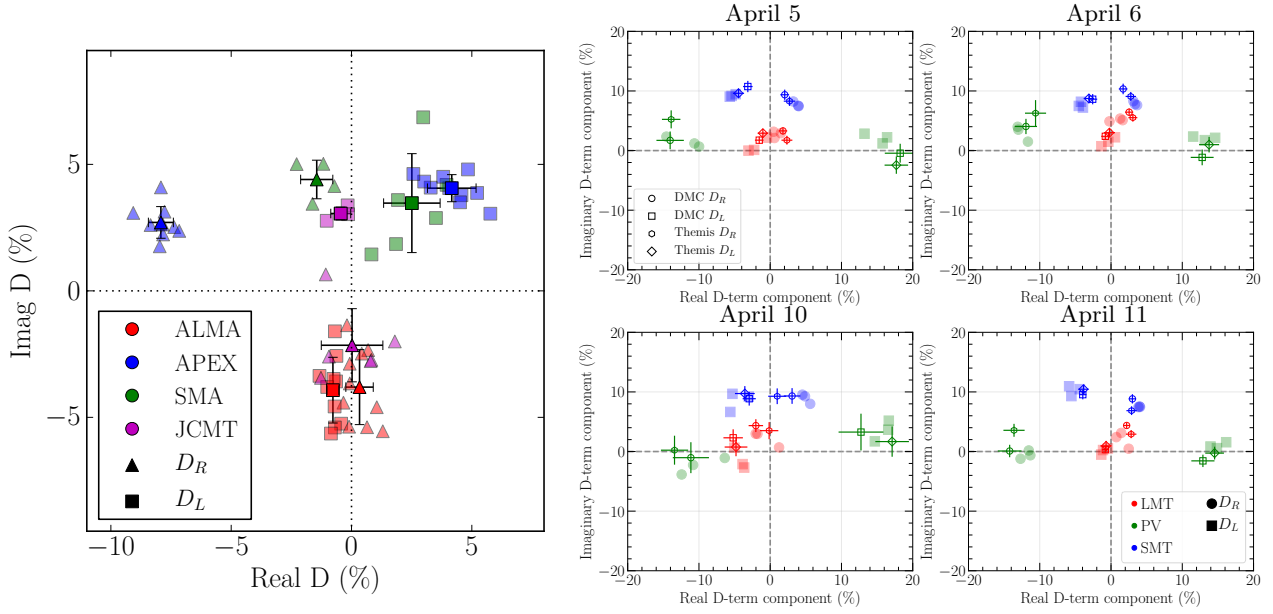
<sup>3</sup> <http://www.aips.nrao.edu>

<sup>4</sup> <https://casa.nrao.edu>

<sup>5</sup> GPCAL is a new automated pipeline written in Python and based on AIPS and the CLEAN imaging software Difmap. GPCAL adopts a similar calibration scheme to LPCAL but allows users to (i) fit the D-term model to multiple calibrators simultaneously and (ii) use more accurate linear polarization models of the calibrators for D-term estimation. In this paper, it is mainly used to complement the LPCAL analysis of the M87 data (Appendix G.3 and K) and the D-term estimation using calibrators (Appendix J).

<sup>6</sup> <https://github.com/achael/eht-imaging>

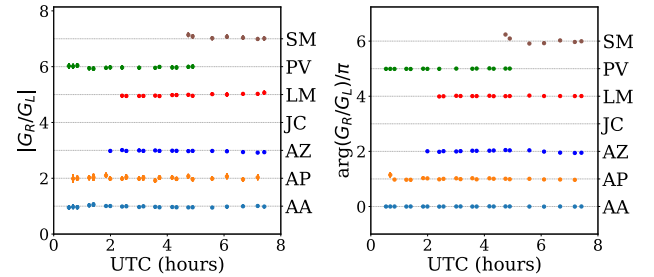




**Figure 2.** *Left panel:* D-term estimates for ALMA, APEX, JCMT, and SMA from `polsolve` multi-source intra-site baseline fitting; one point per day and band (low and high) for each station across the EHT 2017 campaign. Both polarizations are shown for ALMA and APEX per day, one for JCMT and SMA per day due to JCMT polarization setup limitations. Station averages across days, high bands and low bands are shown with error bars. The depicted D-terms are provided in tabulated form in Appendix D. *Right panels:* Fiducial D-terms for LMT, PV, and SMT derived via leakage calibration through **polarimetric imaging methods and posterior modeling** of M87 observations. We depict fiducial D-terms per day, where each point corresponds to one station, polarization, and method. Filled symbols depict D-terms from imaging methods and symbols for posterior exploration methods have errorbars corresponding to the 1- $\sigma$  standard deviations estimated from posterior distributions of the resulting D-terms.

polarimetric **imaging methods** become easier to image and allow methods to focus on accurate reconstructions of polarimetric Stokes  $Q$  and  $U$  brightness distributions and D-term estimation.

Preliminary D-terms estimated via imaging methods are reported in Appendix F. To quantify the agreement (or distance in the complex plane) between D-term estimates from different methods we calculate  $L_1$  norms.  $L_1$  norms averaged over left and right (also real and imaginary) D-term components, over all stations and over time are less than 1% for each pair of imaging methods (see Figure 20 in Appendix E). The mean values of D-term posteriors from the **posterior exploration methods** correlate well with D-terms estimates by **imaging methods**. For each combination of **imaging and posterior exploration method** the station averaged  $L_1$  norms range from 1.5% to 1.89%. Any residual leakage for stations with a co-located partner estimated by LPCAL<sup>7</sup>, and both



**Figure 3.** Amplitudes (left) and phases (right) of the ratio of  $R$  to  $L$  station gains from the DMC fit to M87 April 11 low-band data. Individual station gain ratios are offset vertically for clarity, with the dashed horizontal lines indicating a unit ratio for each station. Note that JCMT only observes one polarization at a time, and so provides no constraints on gain ratios. We see that the assumption made by the **three imaging pipelines and one posterior exploration pipeline (THEMIS)** – namely, that the right- and left-hand gains are equal for all stations at all times – largely seems to hold. The behavior in this plot is representative of that seen across days and bands.

<sup>7</sup> The residual leakage estimated by LPCAL is due to LPCAL being unable to fix D-terms of specific stations to be certain values. Thus, LPCAL obtains solutions for those stations and the non-zero D-terms indicate that there may either be possible residual leakage after zero-baseline fitting or uncertainties in LPCAL estimates originating from e.g., a breakdown of the similarity approximation.

**posterior exploration methods** is small. The gain calibration (see Equation 4) for DMC is shown in Figure 3. As expected, the assumption made by all of the imaging

pipelines and one of the posterior exploration pipelines (THEMIS), that right- and left-hand gains are equal for all stations at all times, holds. For verification purpose, we also estimate D-terms using data of calibrating sources. We find that the D-terms derived by polarimetric imaging of other sources are consistent with those of M87. The results are presented in Appendix J. Finally, our estimated SMT D-terms are similar to those computed previously using EHT observations of Sgr A\* (Johnson et al. 2015).

#### 4.3. Parameter Surveys and Validation on Synthetic Data

Each imaging and leakage calibration method has free parameters that must be set by the user before the optimization or posterior exploration takes place. Some of these parameters (e.g., field of view, number of pixels) are common to all imaging methods, but many are unique to each method (e.g., the sub-component definitions in LPCAL or polysolve, or the regularizer weights in eht-imaging). Often in VLBI imaging, these free parameters are simply set by the user given their experience on similar data sets, or based on what appears to give a good fit to the data free of noticeable imaging artifacts. In this work, we follow Paper IV in choosing the method parameters we use in our final image reconstructions more objectively by surveying a portion of the parameter space available to each method.

We perform surveys over the different free parameters available to each imaging method and attempt to choose an optimal set of parameters based on their performance faithfully recovering the source structure and input D-terms from our synthetic data models. The parameter set that performs best on the synthetic data for each method is considered our “fiducial” parameter set for imaging M87 with that method. The corresponding images reconstructed from various data sets using these parameters are the method’s “fiducial images”.

The synthetic data sets we used for scoring the imaging parameter combinations consist of six synthetic EHT observations using the M87 April 11 equivalent low band ( $u, v$ ) coverage. The source structure models used in the six sets vary from complex models for source structure generated using general relativistic magnetohydrodynamics (GRMHD) simulations of M87’s core and jet base (Models 1 and 2 from Chael et al. 2019) to simple geometrical models (a filled disk, Model 3, and simple rings with differing EVPA patterns, Models 4-6). The synthetic source models have varying degrees of fractional polarization and diverse EVPA structures. The mock data source models blurred to the EHT nominal resolution are displayed in the first column of Figure 4.

All M87 synthetic data sets were generated using the synthetic data generation routines in eht-imaging. We followed the synthetic data generation procedure in Appendix C.2 of Paper IV, but with models featuring com-

plex polarization structure. The synthetic visibilities sampled on EHT baselines are corrupted with thermal noise, phase and gain offsets, and polarimetric leakage terms. Mock D-terms for the SMT, LMT, and PV stations were chosen to be similar to those found by the initial exploration of the M87 EHT2017 data reported in Appendix F. Random residual D-terms for ALMA, APEX, JCMT, and SMT (reflecting possible errors in the zero-baseline calibration procedure) were drawn from normal distributions with 1% standard deviation. After generation, the phase and amplitude gains in the synthetic data were calibrated for use in imaging pipelines in the same way as the real M87 data; that is, they were self-calibrated to a Stokes  $\mathcal{I}$  image reconstructed via the SMILI fiducial script for M87 developed in Paper IV.

In Figure 4, we present our fiducial set of images (in a uniform scale) from synthetic data surveys carried within each method. In each panel we report a correlation coefficient  $\langle I \cdot I_0 \rangle$  between recovered Stokes  $\mathcal{I}$  and the ground truth  $\mathcal{I}_0$  images,

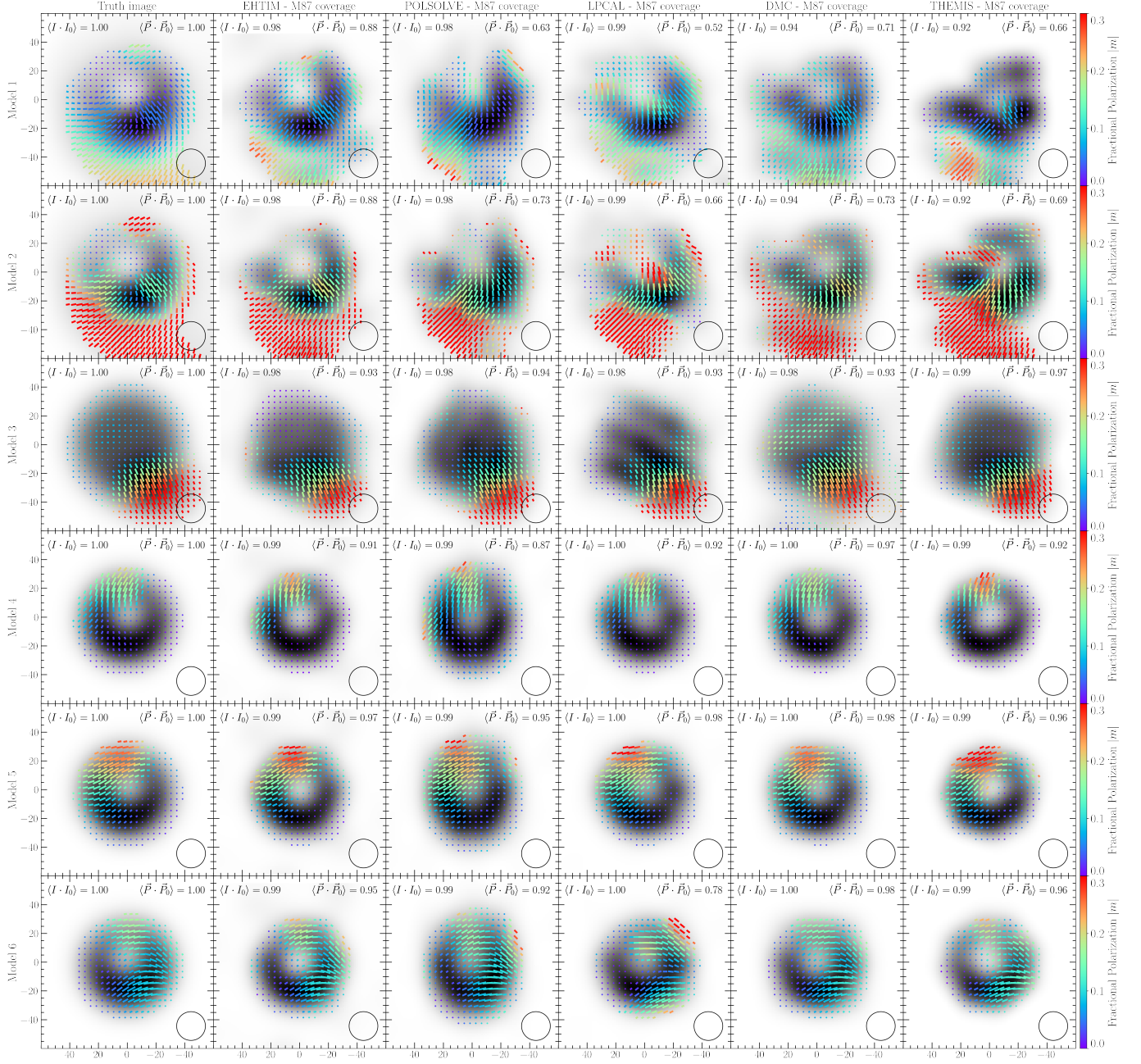
$$\langle I \cdot I_0 \rangle = \frac{\langle (I - \bar{I})(I_0 - \bar{I}_0) \rangle}{\sqrt{\langle (I - \bar{I})^2 \rangle} \sqrt{\langle (I_0 - \bar{I}_0)^2 \rangle}}. \quad (8)$$

This reflects the dot product of the two mean-subtracted images when treated as unit vectors. We also calculate a correlation coefficient for the reconstructed linear polarization image  $p \equiv \mathcal{Q} + i\mathcal{U}$ ,

$$\langle \vec{P} \cdot \vec{P}_0 \rangle = \frac{\text{Re}[\langle p p_0^* \rangle]}{\sqrt{\langle p p^* \rangle} \sqrt{\langle p_0 p_0^* \rangle}}. \quad (9)$$

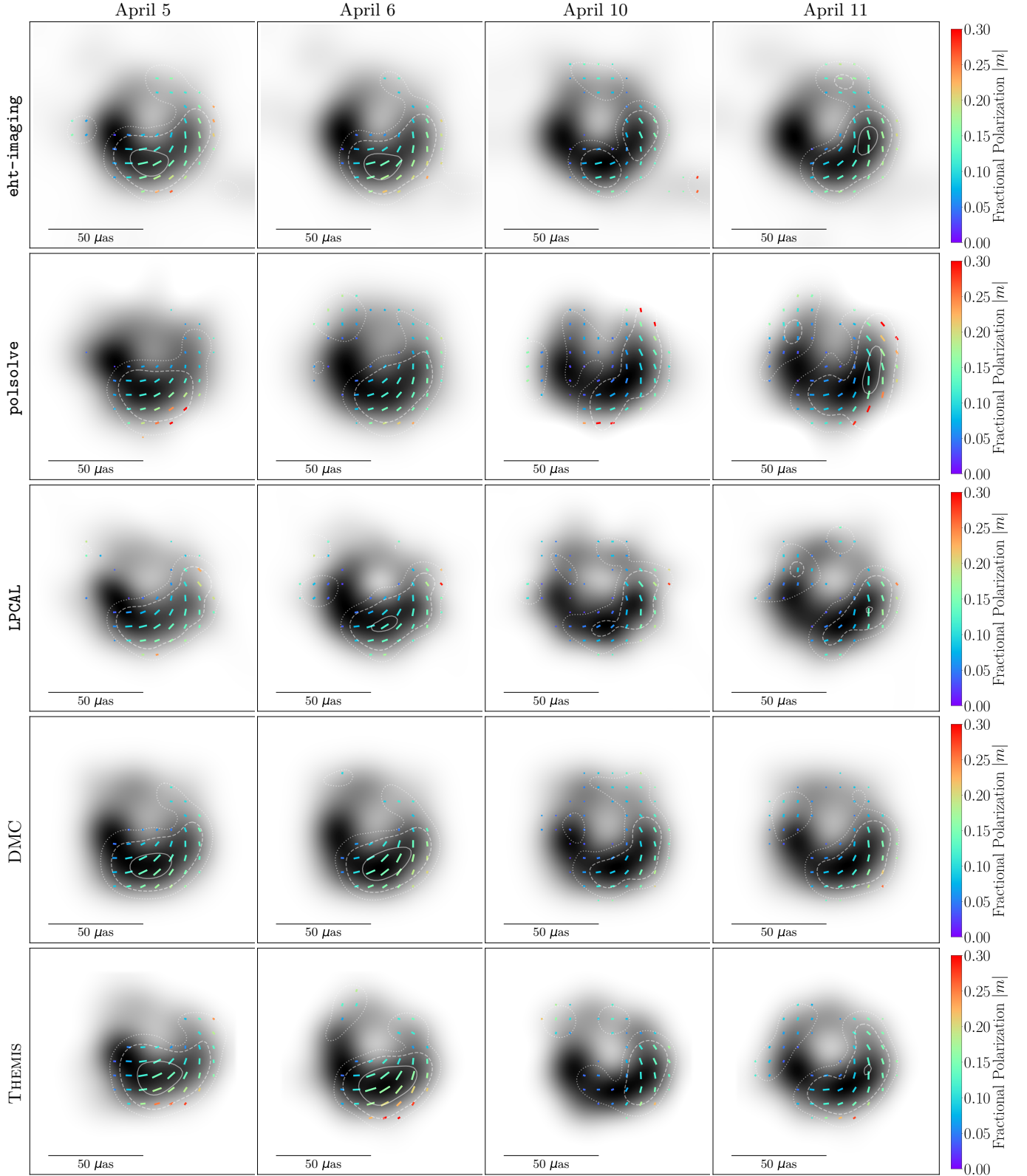
The real part is chosen to measure the degree of alignment of the polarization vectors ( $\mathcal{Q}, \mathcal{U}$ ). In both cases, images are first shifted to give the maximum correlation coefficient for Stokes  $\mathcal{I}$ . Because Stokes  $\mathcal{I}$  image reconstructions are tightly constrained by an a priori known total image flux, the Stokes  $\mathcal{I}$  correlation coefficients are mean subtracted to increase the dynamic range of the comparison. This introduces a field of view dependence to the metric, as only spatial frequencies above (field of view)<sup>-1</sup> are considered; up to the beam resolution. There is no such dependence in the linear polarization coefficient which is not mean subtracted.

The correlation is equally strong independently of the employed method. The polarization structure is more difficult to recover for models with high or complex extended polarization (Models 1 and 2) for which correlation of the recovered polarization vectors is strong to moderate. This seems to be independent of the method as well. In Figure 5 we present a uniform comparison of the recovered D-terms and the ground truth D-terms for all synthetic data sets and methods. For all methods the recovered D-terms show a strong correlation with the model D-terms. To quantify the agreement (or distance in the complex plane) between D-term estimates

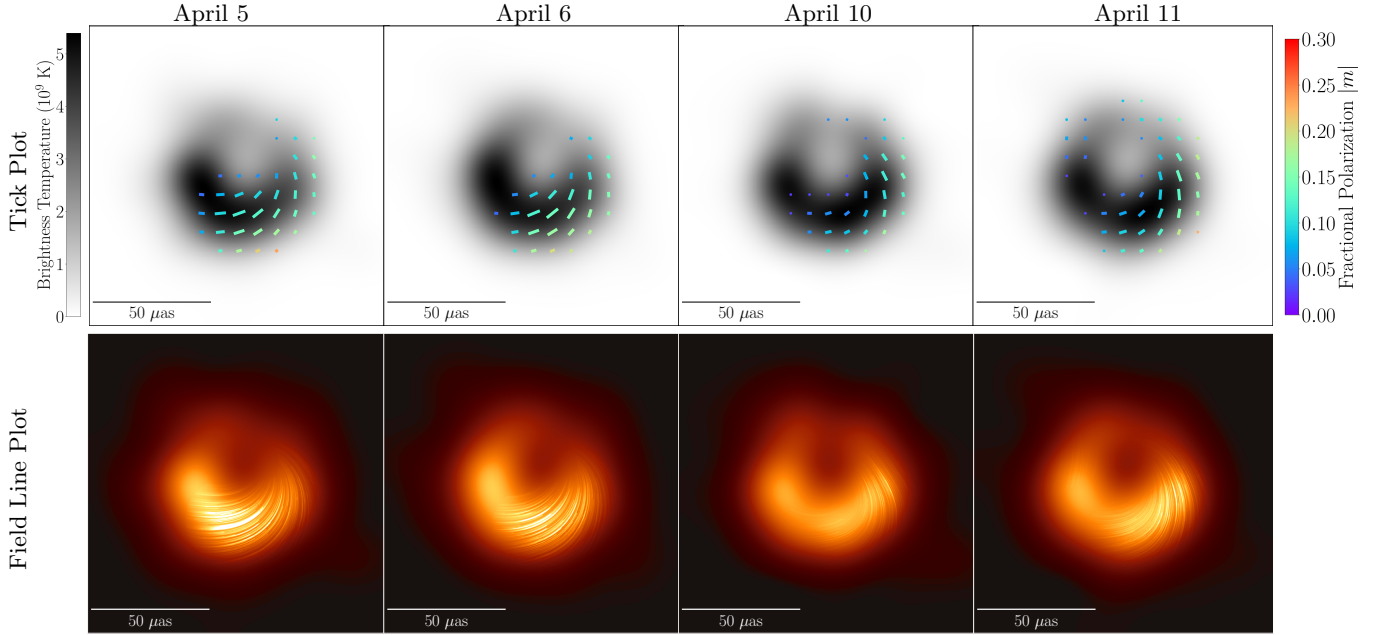


**Figure 4.** Fiducial images from synthetic data model reconstructions using M87 April 11 low band  $(u, v)$  coverage. Rows from top to bottom correspond to six different synthetic data sets. Columns from left to right show ground truth synthetic image (column 1) and the best image reconstructions by each method (columns 2-6). The polarization tick length reflects total linear polarization, while the color reflects fractional polarization from 0 to 0.3. The normalized overlap is calculated against the respective ground truth image, and in the case of the total intensity it is mean-subtracted.





**Figure 6.** Fiducial M87 images produced by five independent methods. Results from **all imaging and posterior exploration pipelines** are shown on all four M87 low-band observation days (low and high band results are consistent, [see Appendix I](#)). Total intensity is shown in grayscale, polarization ticks indicate the EVPA, the tick length indicates linear polarization intensity magnitude, and color indicates fractional linear polarization. The tick length is scaled according to the polarized brightness without renormalization to the maximum for each image. The contours mark linear polarized intensity. The solid, dashed, and dotted contour levels correspond to linearly polarized intensity of 20, 10, and  $5 \mu\text{Jy}/\mu\text{as}^2$ . Cuts were made to omit all regions in the images where Stokes  $\mathcal{I} < 10\%$  of the peak flux density and  $p < 20\%$  of the peak polarized flux density. The images are all displayed with a field of view of  $120 \mu\text{as}$ , and all images were brought to the same nominal resolution by convolution with the circular Gaussian kernel that maximized the cross-correlation of the blurred Stokes  $\mathcal{I}$  image with the consensus Stokes  $\mathcal{I}$  image of [Paper IV](#).



**Figure 7.** Fiducial M87 average images per day produced by averaging results from our five methods (see Figure 6). Method-average images for all four low-band M87 observation days are shown, from left to right (**low and high band results are consistent, see Appendix I**). We employ here two visualization schemes (top and bottom) to display our four method-average images. The images are all displayed with a field of view of  $120 \mu\text{as}$ , and all images were brought to the same nominal resolution by convolution with the circular Gaussian kernel that maximized the cross-correlation of the blurred Stokes  $\mathcal{I}$  image with the consensus Stokes  $\mathcal{I}$  image of Paper IV. *Top:* Total intensity, polarization fraction, and EVPA are plotted in the same manner as in Figure 6. *Bottom:* Polarization “field lines” plotted atop an underlying total intensity image. Treating the linear polarization as a vector field, the sweeping lines in the images represent streamlines of this field and thus trace the EVPA patterns in the image. To emphasize the regions with stronger polarization detections, we have scaled the length and opacity of these streamlines as the square of the polarized intensity. This visualization is inspired in part by Line Integral Convolution (LIC; Cabral & Leedom 1993) representations of vector fields, and it aims to highlight the newly added polarization information on top of the standard visualization for our previously published Stokes  $\mathcal{I}$  results (Paper I; Paper IV).

on the remaining statistical uncertainties in our leakage calibration. In addition, the different assumptions and parameters used in each imaging method affect the recovered polarized intensity pattern, introducing an additional source of systematic uncertainty in our recovered images. In this section, we assess the consistency of the recovered polarized images across different D-term calibration solutions within and between methods.

We explore the consistency of our image reconstructions against the uncertainties in the calibrated D-terms by generating a sample of 1000 images for each method, each generated with a different D-term solution. For the **imaging methods**, we define complex normal distributions for each D-term based on the results of Figure 2 and reconstruct images after calibrating to each set of random D-terms. This procedure is explained in detail in Appendix H. For the **posterior exploration methods** we simply draw 1000 images from the posterior for each observing day.

For each method’s set of 1000 image samples covering a range of D-term calibration, we study the azimuthal distribution of the polarization brightness ( $p$ ) and EVPA ( $\chi$ ) by performing intensity-weighted averages of these

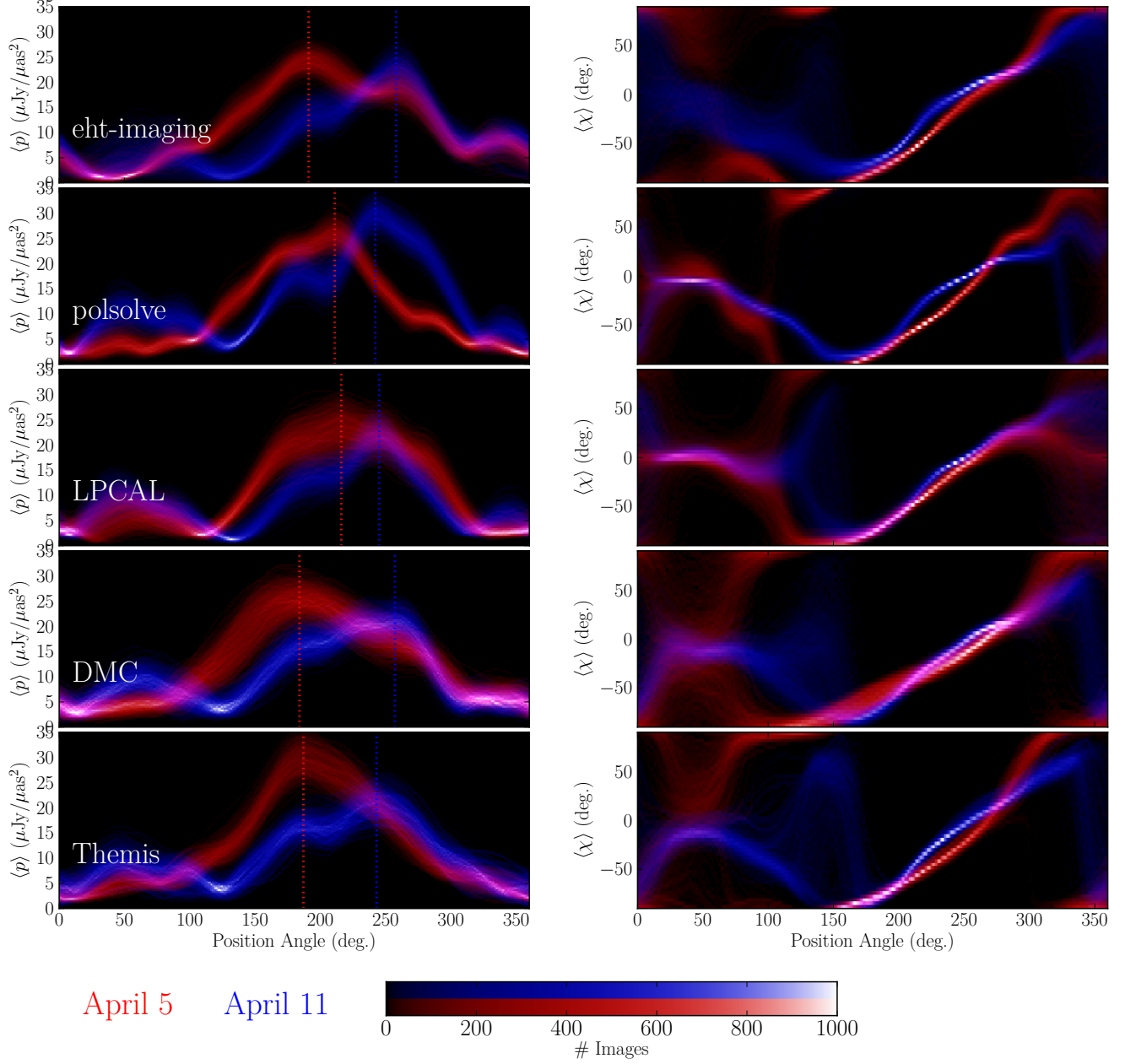
quantities over different angular sections along the ring. The width of the angular sections used in the averaging is set to  $\Delta\varphi = 10^\circ$  and the averages are computed from a position angle  $\varphi = 0^\circ$  to  $\varphi = 360^\circ$ , in steps of  $1^\circ$ .

Comparing angular averages of these quantities with a small moving window  $\Delta\varphi$  avoids spurious features from e.g., the different pixel scales used in the different image reconstruction methods. The pixel coordinates of the image center are estimated (for each method) from the peak of the cross-correlation between the  $\mathcal{I}$  images and the representative images of M87 used in the self-calibration. To avoid the effects of phase wrapping in the averaging (which biases the results for values of  $\chi$  around  $\pm 90^\circ$ ), the quantity  $\langle\chi\rangle$  is computed coherently within each angular section, i.e., the averages are defined as

$$\langle p \rangle \equiv \frac{\langle \mathcal{I} \sqrt{\mathcal{Q}^2 + \mathcal{U}^2} \rangle}{\langle \mathcal{I} \rangle}, \quad (10)$$

$$\langle \chi \rangle \equiv \frac{1}{2} \arctan \left( \frac{\langle \mathcal{Q} \times \mathcal{I} \rangle}{\langle \mathcal{U} \times \mathcal{I} \rangle} \right). \quad (11)$$





**Figure 8.** Histograms of the azimuthal distributions of polarized intensity (left) and EVPA (right) obtained from the Monte Carlo D-term analysis with **all imaging and posterior exploration methods**. These quantities are estimated as the intensity-weighted averages within an angular section of a width of 10 deg. The position angle is measured counter-clockwise, starting from North. The position angles with highest average polarization brightness are marked with dotted lines for each method and day.







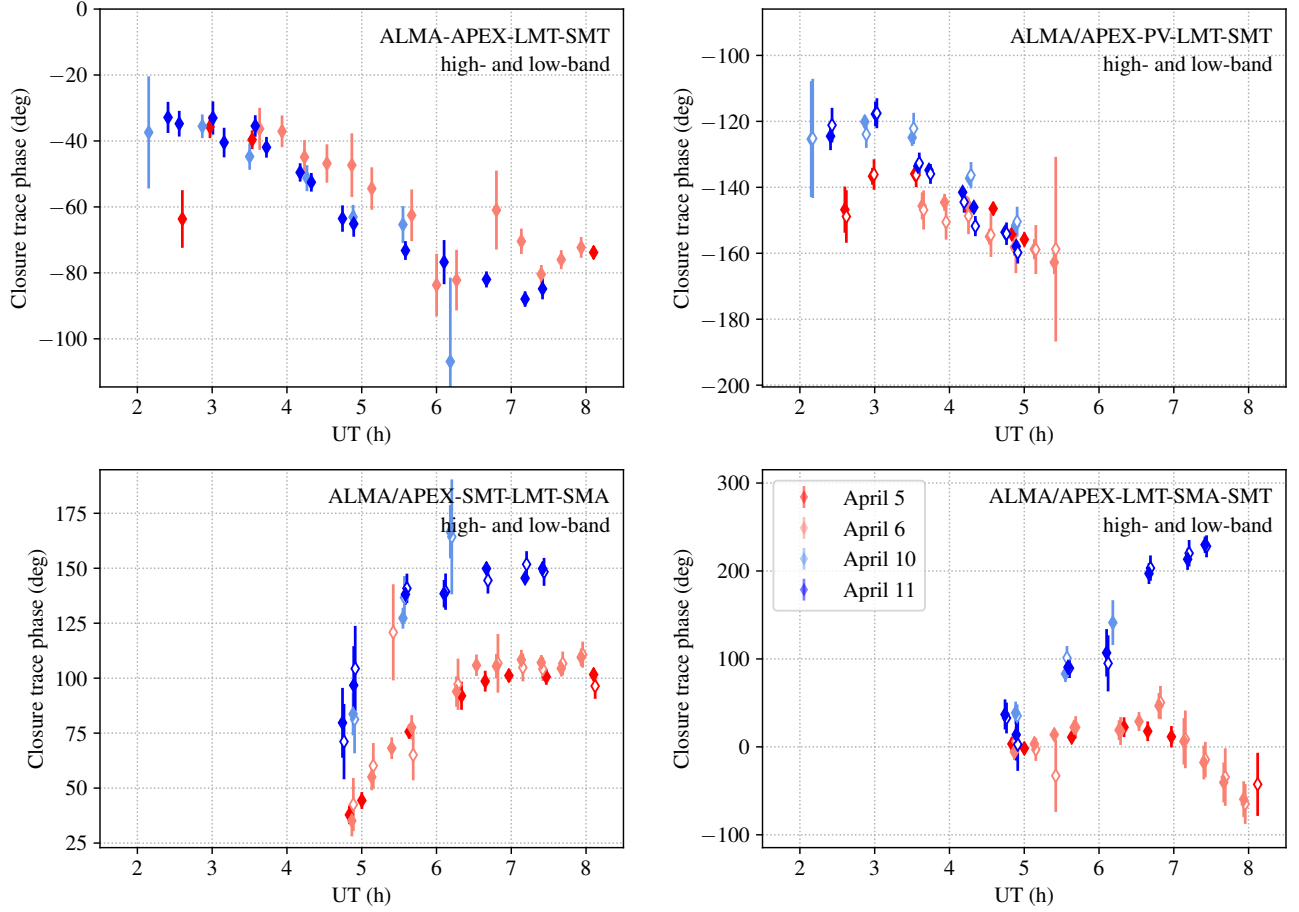




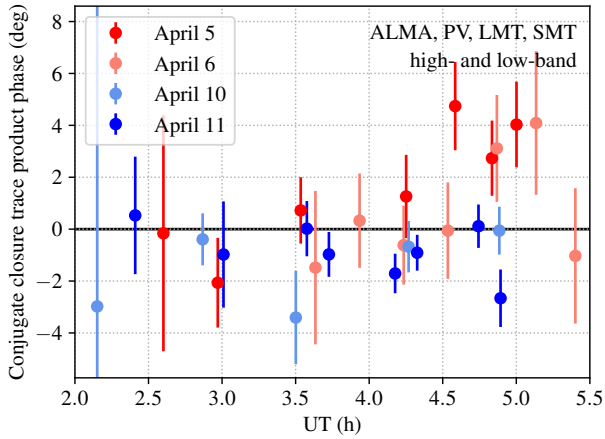








**Figure 14.** Phases of M87 closure traces on four illustrative quadrangles for the different observation days. Closure traces constructed with ALMA and APEX are shown by filled and open points, respectively. The plotted closure traces represent an average across high- and low-band data. An  $S/N > 1$  selection in the final closure trace phase has been applied.



**Figure 15.** Phase of conjugate closure trace products constructed on the ALMA-PV-LMT-SMT and ALMA-SMT-LMT-PV quadrangles, averaged across high- and low-bands for each of the days on which M87 was observed.

the Fourier-transformed model brightness matrix (Equations 6 and 4). The total number of parameters used in

this fit is equal to two times the the number of source sub-components (i.e.,  $2N$ , which correspond to  $q_i$  and  $u_i$  in  $Q(\mathbf{x}) = \sum_i^N q_i \mathcal{I}_i(\mathbf{x})$  and  $U(\mathbf{x}) = \sum_i^N u_i \mathcal{I}_i(\mathbf{x})$ ) plus four times the number of antennas (i.e.,  $4N_a$ , accounting for the real and imaginary parts of the  $D_R$  and  $D_L$  of each antenna). The error function (or log-likelihood) to be minimized is the sum of the  $\chi^2$  values computed for the cross-polarization matrix elements of the RIME, i.e.,

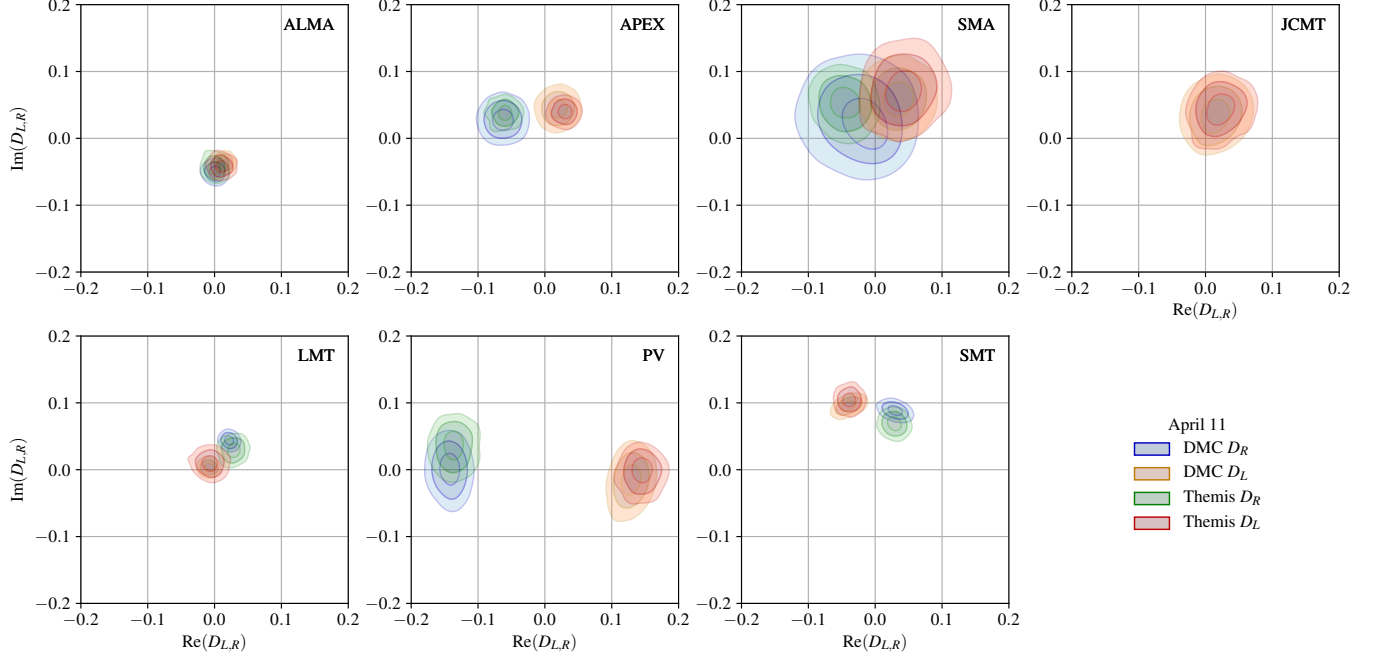
$$\chi^2 = \sum_m^{N_v} w_m \left| RL_{kl,m}^c - \left( \tilde{Q} + i\tilde{U} \right)_m \right|^2 + \sum_m^{N_v} w_m \left| LR_{kl,m}^c - \left( \tilde{Q} - i\tilde{U} \right)_m \right|^2, \quad (C4)$$

where  $w_m$  is the weight of the  $m$ -th visibility, the index  $c$  stands for calibrated visibilities (corrected both for station gains and for instrumental polarization using the current estimate of the D-terms) and  $N_v$  is the number of visibilities.

The calibrated visibilities,  $RL_{kl,m}^c$  and  $LR_{kl,m}^c$ , depend on  $D_R^k$ ,  $D_L^k$ ,  $D_R^l$  and  $D_L^l$  (Equation 4), whereas  $\tilde{Q}$







**Figure 16.** Leakage posteriors for individual stations from DMC and THEMIS reconstructions of M87 on April 11. Because JCMT only records a single polarization, only lefthand D-terms are shown. The plotted contours enclose 50%, 90%, and 99% of the posterior probability, and show a large degree of overlap for all stations despite considerable differences in the underlying model specifications.

on the gain phases. The right- and left-hand leakage amplitudes are sampled from a unit uniform prior, and the leakage phases are sampled from a wrapped uniform prior.

The DMC likelihood variances are set to the quadrature sum of the data thermal variances and a systematic component that is modeled as the square of a fraction of the Stokes  $\mathcal{I}$  visibility amplitude; this fractional uncertainty parameter is sampled from a unit uniform prior.

### C.3.2. THEMIS

The existing imaging method described in Broderick et al. (2020a) has been extended to polarization reconstructions. This makes use of a deterministic even-odd swap tempering scheme (Syed et al. 2019) using the HMC sampling kernel from the Stan package (Carpenter et al. 2017). Here we briefly summarize the implementation and assumptions underlying the THEMIS polarization map reconstructions; more detail on these points will be presented elsewhere (A. E. Broderick et al. *in prep.*).

As with DMC, all THEMIS analyses are performed on coherently scan-averaged visibility data. Unlike the DMC analysis, intrasite baselines are included to facilitate gain and leakage calibration. This is enabled by the inclusion of a large, uniformly polarized Gaussian to model the milliarcsecond-scale structure (see, e.g., Broderick et al. 2020a; Paper IV).

THEMIS models the polarized image as a small number of control points located on a rectilinear grid, from which the fields  $\mathcal{I}$ ,  $\ell$ ,  $\xi$ , and  $\cos(\varsigma)$  are constructed via an approximate cubic spline in a fashion similar to Broderick et al. (2020a). The field of view and orientation of the rectilinear grid are fit parameters and permitted to vary. In this way the effective resolution is reconstructed from the data itself. Logarithmic priors are adopted on  $\mathcal{I}$  and  $\ell$ , flat priors are adopted on  $\xi$  and  $\cos(\varsigma)$  with the natural limits.

Complex station gains are reconstructed via the Laplace approximation (see Section 6.8 of Broderick et al. 2020b). The right- and left-hand complex station gains are constrained to be equal, and permitted to vary independently on every scan. Log-normal priors are imposed on the station gain amplitudes. The real and imaginary components of the right- and left-hand leakages are treated as additional model parameters, with each component sampled uniformly on  $[-1, 1]$ .

Unless otherwise indicated, THEMIS analyses shown here used a  $5 \times 5$  raster grid, consistent with that typically necessary to capture features on the scale of the EHT beam within the field of view imposed by the shortest intersite baselines. A 3% systematic noise component was added in quadrature to the thermal uncertainties to capture non-closing errors in the scan-averaged visibilities. These are similar to the magnitude of fractional systematic error inferred from the DMC analyses.



averaged products from intra-band leakage studies for ALMA–APEX.

Simultaneously to our VLBI observations, ALMA also observes as an interferometric array (referred to as ALMA-only) in a linear-polarization basis. This array data is used for ALMA-VLBI calibration in the Quality Assurance process at ALMA (QA2; Goddi et al. 2019), and provides source-integrated information for calibration refinement and validation, such as total flux densities or polarization properties. Given that our intra-site baselines do not resolve the observed sources, the source-integrated properties from ALMA–APEX, SMA–JCMT and the core component of ALMA-only should match. We show our validation of the derived source polarimetric properties from the intra-site D-term fitting against QA2 ALMA-only estimates in the left (for  $Q$ ) and center (for  $U$ ) panels of Figure 17. There is a strong correlation between the Stokes parameters of all sources derived from the ALMA-only observations (Goddi et al. 2019) and the estimates from the ALMA–APEX intra-site VLBI baseline. This correlation can be seen as a further validation test of the quality of the EHT polarimetric calibration.

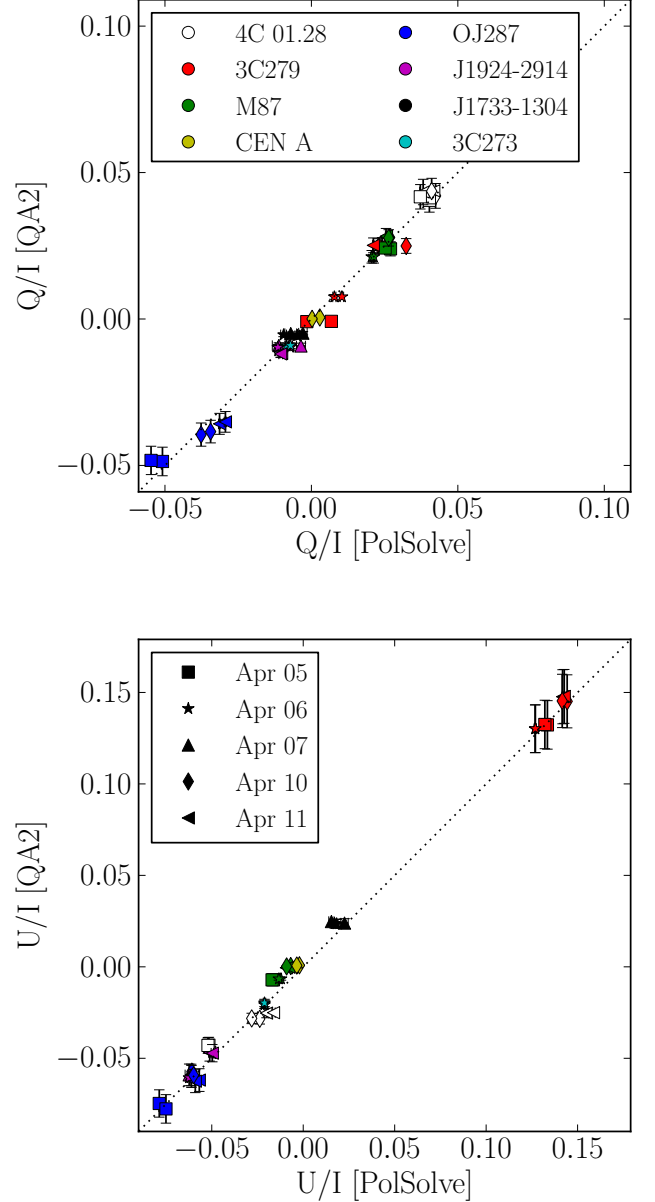
The polarimetric leakage of the SMA is well characterized, with D-terms of only a few percent expected for observations near the 233.0 GHz tuned frequency of the quarter-wave plates (Marrone 2006; Marrone & Rao 2008). In addition to historical measurements of leakage, near-in-time polarimetric observations of sources with the SMA also allowed us to compute quasi-simultaneous leakage estimates that can be compared with our intra-site method estimates. Observations of 3C 454.3, M87, and 3C 279 within a month of our EHT campaign provided an upper limit of 10% for D-terms, consistent with our intra-site method estimates, and stable across days at the 1% level.

We also validated the `polsolve` leakage estimates using point-source modeling within the `eht-imaging` and DMC libraries. Both modeling schemes assume a constant polarization fraction and EVPA for the point source. The DMC model fits to cross-hand and parallel-hand visibilities by incorporating right- and left-hand station gains as model parameters, while the `eht-imaging` model fits to gain-independent “polarimetric closure” data products consisting of the ratio of cross-hand visibilities to parallel-hand visibilities on a single baseline (see, e.g., Blackburn et al. 2020),

$$\mathcal{K}_{jk} = \frac{R_j L_k^* \times L_j R_k^*}{R_j R_k^* \times L_j L_k^*}. \quad (\text{D8})$$

Both models use Gaussian likelihood functions for their respective data products.

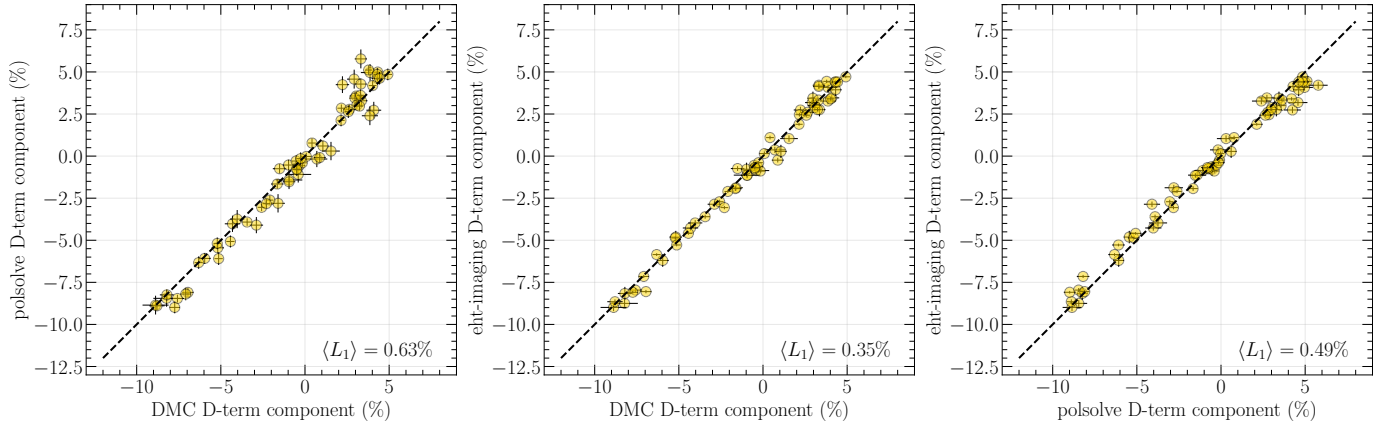
In Figure 18 we compare the multi-source `polsolve` leakage estimates to multi-source `eht-imaging` fits and single-source (using 3C 279) DMC fits; both `eht-imaging` and DMC have fit only to the ALMA–APEX baseline, while the `polsolve` estimates addition-



**Figure 17.** Comparison of source-integrated Stokes  $Q$  and  $U$  estimates from intra-site EHT baselines using the multi-source fitting mode of `polsolve` to those from ALMA-only observations (Goddi et al. 2019).

ally fit to the SMA–JCMT baseline. We find that the leakage terms recovered by all three methods are consistent with one another, with an uncertainty-weighted mean absolute deviation across all days and bands of  $<1\%$  in absolute leakage between any two methods.

Furthermore, our leakage estimation methods used band-averaged data products. Given the high S/N of the detections between ALMA and APEX, there are strong detections in all four correlation products (i.e.,  $RR$ ,  $RL$ ,



**Figure 18.** Pairwise comparisons of leakage estimates for ALMA and APEX, obtained from point-source modeling of the intra-site baseline with **polsolve**, **eht-imaging**, and DMC. Both **polsolve** and **eht-imaging** leakages are derived from multi-source fits, while the DMC leakages are derived from fitting to 3C 279 only. Each panel aggregates leakage estimates from both stations (ALMA and APEX), both bands, and all four observing days. Values quoted in the lower right-hand corner of each panel are the uncertainty-weighted mean absolute deviation for the corresponding pair of fits. The dashed line on each plot marks where  $y = x$ .

$LR$  and  $LL$ ) at each intermediate frequency band<sup>12</sup>. We can therefore use the high S/N on ALMA–APEX to estimate the D-terms at each intermediate frequency band and study the possible frequency dependence of the instrumental polarization of ALMA and APEX. The results are shown in Figure 19. This test showed very stable D-term estimates across the entire band, motivating band-averaging.

#### E. FIDUCIAL LEAKAGE D-TERMS FROM M87 IMAGING

We provide fiducial M87 D-term estimates for each method in Table 5. The D-terms for LMT, SMT, and PV are depicted in Figure 2. In Figure 20 we show an example of one-to-one software comparisons of the campaign-average D-terms for LMT, PV and SMT.

#### F. PRELIMINARY IMAGING RESULTS FOR M87

In this appendix we present the preliminary polarimetric results on M87 obtained using the three imaging methods. These preliminary images were generated “by hand”, with manual tuning of free parameters in the imaging and calibration process, before full parameter surveys were done to choose parameters more objectively and evaluate uncertainties. Nonetheless, in this early stage of imaging we found a high degree of similarity in the recovered structure and D-terms between methods; these results guided the design of our synthetic data tests and parameter survey strategy we pursued to obtain our final polarimetric images of M87.

The preliminary polarimetric imaging and leakage calibration used the April 11 pre-processed data set (Stokes

$\mathcal{I}$  self-calibrated and leakage correction applied for stations with a co-located partner) are not blind tests in analogy to total intensity imaging (see Paper IV). In this preliminary step, parameters used in the methods were hand-tuned by expert users. This preliminary imaging demonstrates that the total intensity image recovered from the pre-processed data set is roughly consistent with the original Stokes  $\mathcal{I}$  image without script fine-tuning.

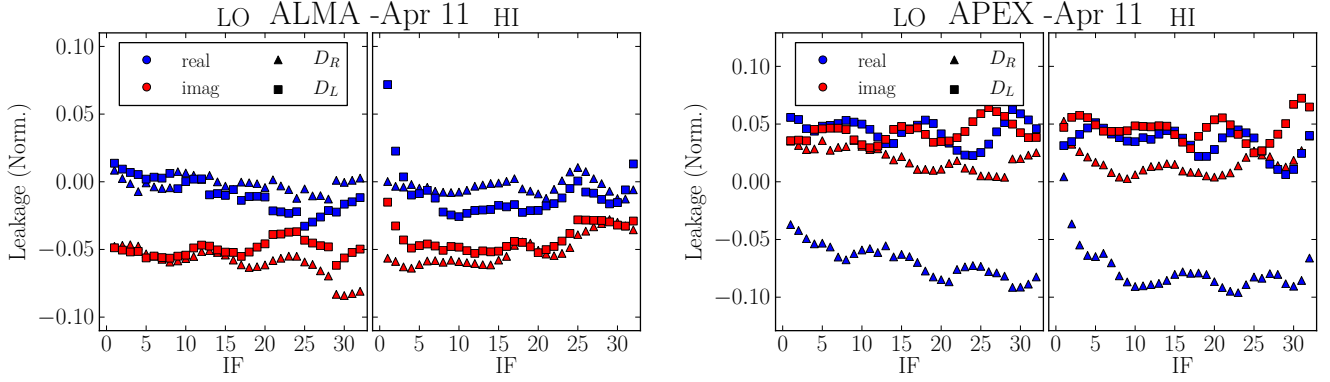
In Figure 21, we present our recovered total intensity and preliminary polarimetric images of M87 on April 11 produced by the three chosen methods. In Figure 21, we also show D-terms associated with these images. Each method reproduces consistent D-terms for all remaining long-baseline EHT stations. The preliminary polarimetric images are roughly consistent across methods. In all images, the M87 ring-like structure is predominantly polarized mostly in the south–west part with a fractional polarization of about  $|m| \sim 15\%$ . The EVPAs are organized into a coherent pattern along the ring. However, small differences in fractional polarization and polarized flux density are evident between the three packages. The preliminary results strongly motivate the need for a full parameter survey for each introduced method.

#### G. DESCRIPTION OF THE PARAMETER SURVEY AND SCORING FOR EACH METHOD

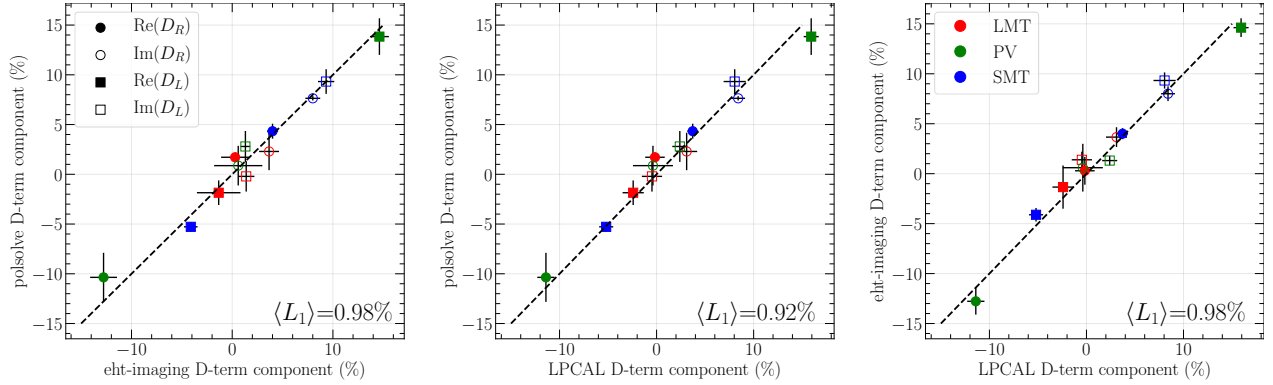
In what follows, we describe each method’s approach to surveying the space of free parameters available to it, scoring the results using these six synthetic data models, and from these scores, determining a fiducial set of parameters to use in the final polarimetric imaging of M87. We use each method’s fiducial parameter settings to obtain the final M87 images and calibrated D-terms.

<sup>12</sup> In the VLBI correlation, each 2 GHz band is divided into 32 contiguous sub-bands of equal width, which are called “intermediate frequency bands”, or IFs.

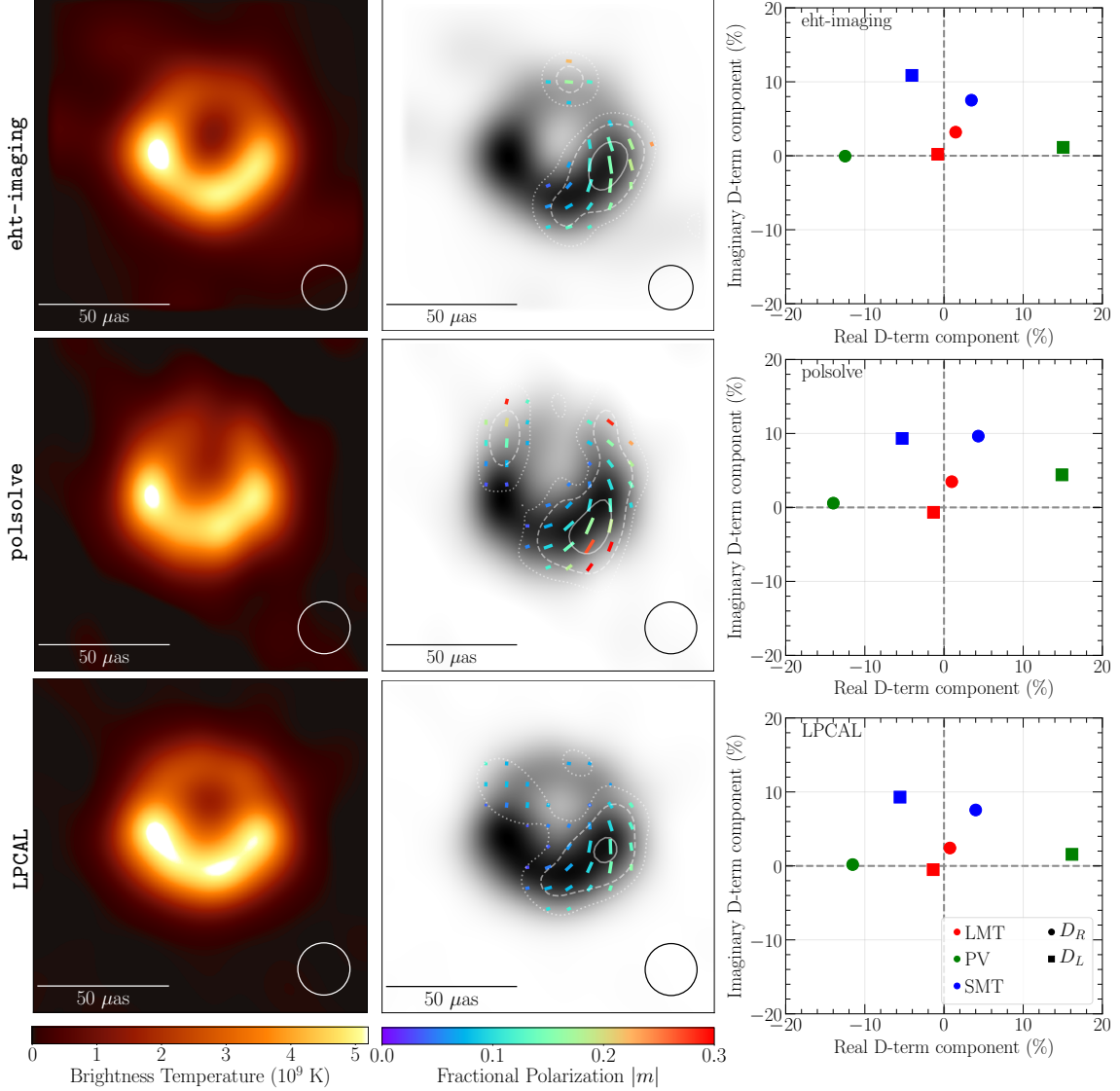




**Figure 19.** ALMA (left) and APEX (right) D-term spectra recovered on April 11. Each band has a width of 2 GHz and is divided into 32 intermediate frequency sub-bands (IFs) of equal width.



**Figure 20.** Example one-to-one software comparisons of the campaign-average D-term estimates for LMT, PV, and SMT polarimetric imaging and leakage calibration of M87 observations. Left: Comparison of `eht-imaging` estimates against `polysolve` estimates. Center: Comparison of `LPCAL` estimates against `polysolve` estimates. Right: Comparison of `LPCAL` estimates against `eht-imaging` estimates. Norm  $L_1$  is averaged over left, right, real, imaginary components of the D-terms and over all shown EHT stations. See section 4.2 for averaged Norm  $L_1$  between `eht-imaging`/`polysolve`/`LPCAL` and THEMIS/DMC.



**Figure 21.** *Left:* Preliminary April 11 total intensity images reconstructed with **eht-imaging**, **polsolve**, and **LPCAL**. **eht-imaging** images are blurred with a  $17.1\mu\text{as}$  circular Gaussian, to obtain an equivalent resolution to the **polsolve** and **LPCAL** CLEAN images restored with a  $20\mu\text{as}$  circular Gaussian. *Middle:* Corresponding polarimetric reconstructions obtained as a result of the full-array leakage calibration. Total intensity is shown in the background in grayscale. Polarization ticks indicate the EVPA, the tick length is proportional to the linear polarization intensity magnitude, and color indicates fractional linear polarization. The contours mark linear polarized intensity. The solid, dashed, and dotted contour levels correspond to linearly polarized intensity of 20, 10, and  $5\mu\text{Jy}/\mu\text{as}^2$ . Cuts were made to omit all regions in the images where Stokes  $\mathcal{I} < 10\%$  of the peak flux density and  $p < 20\%$  of the peak polarized flux density. In all reconstructions, the region with the highest linear polarization fraction and polarized intensity is predominantly in the south-west portion of the ring. *Right:* Preliminary D-terms for SMT, PV, and LMT derived via leakage calibration through **eht-imaging**, **polsolve**, and **LPCAL** polarimetric imaging.

### G.1. *eht-imaging* parameter survey

The polarimetric imaging procedure alternates between imaging via minimization of the objective function (Equation C6) and D-term calibration, as described in Section C.2. In the imaging stage, the critical parameters that influence the final reconstruction include the four hyperparameters  $\alpha_P$ ,  $\alpha_m$ ,  $\beta_{HW}$ , and  $\beta_{TV}$  that set the relative weighting in the objective function between

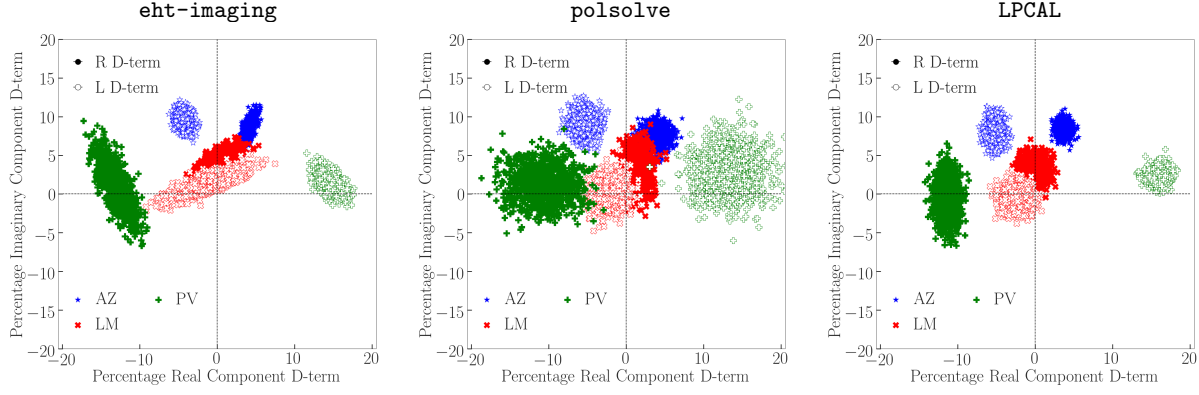
the different data constraints and regularizing terms. In surveying different parameters in the **eht-imaging** survey, we fix  $\alpha_m = 1$  and vary the other three hyperparameter weights.

In addition to the hyperparameter weights, an additional free parameter in our objective function is the amount of additional systematic noise to add to the data as a budget for non-leakage sources of systematic errors









**Figure 24.** Samples of 1000 SMT, LMT, and PV D-terms applied to the data and used in each of the three image reconstruction algorithms in the Monte-Carlo procedure described in Section 5.2. Each D-term was drawn from a normal distribution with no correlations between the D-terms. The means and (co)variances of these distributions for each method were determined from the set of four fiducial D-term solutions found across the four observing days for each method. **eht-imaging** included covariance between the real and imaginary parts of each D-term in its approach, while **LPCAL** and **polysolve** did not.

Model 1 and 2 synthetic data reconstructions, the number of control points were incrementally increased until acceptable fits were obtained.

#### H. D-TERM MONTE CARLO SURVEY DETAILS

In this Appendix, we discuss the procedure we follow to assess the consistency of the images to uncertainties in the D-term calibration from the three non-MCMC image reconstruction methods (**eht-imaging**, **LPCAL**, and **polysolve**). We use this method to generate a sample of 1000 images with different D-term calibration solutions for each method on each observing day. These samples are used to assess our uncertainty in the polarimetric image structure in Section 5.2 and Section 5.3.

##### H.1. Method

Our method is to use a simple Monte-Carlo approach, similar to the analysis of Martí-Vidal et al. (2012) to study the coupling between antenna D-terms and the recovered polarimetric source structure. For each method, we draw 1000 random sets of D-terms from normal distributions with means and (co)variances determined by considering the fiducial results from Table 5 across the four observing days. We assume for this test that the uncertainties in the D-terms are uncorrelated from station to station and between LCP and RCP. This represents a worst-case scenario test, since correlations between the D-terms would reduce the volume of the D-term parameter space surveyed by each method. The full sample of 1000 D-term sets sampled for the SMT, LMT, and PV on April 11 for **eht-imaging**, **polysolve**, and **LPCAL** are shown in Figure 24.

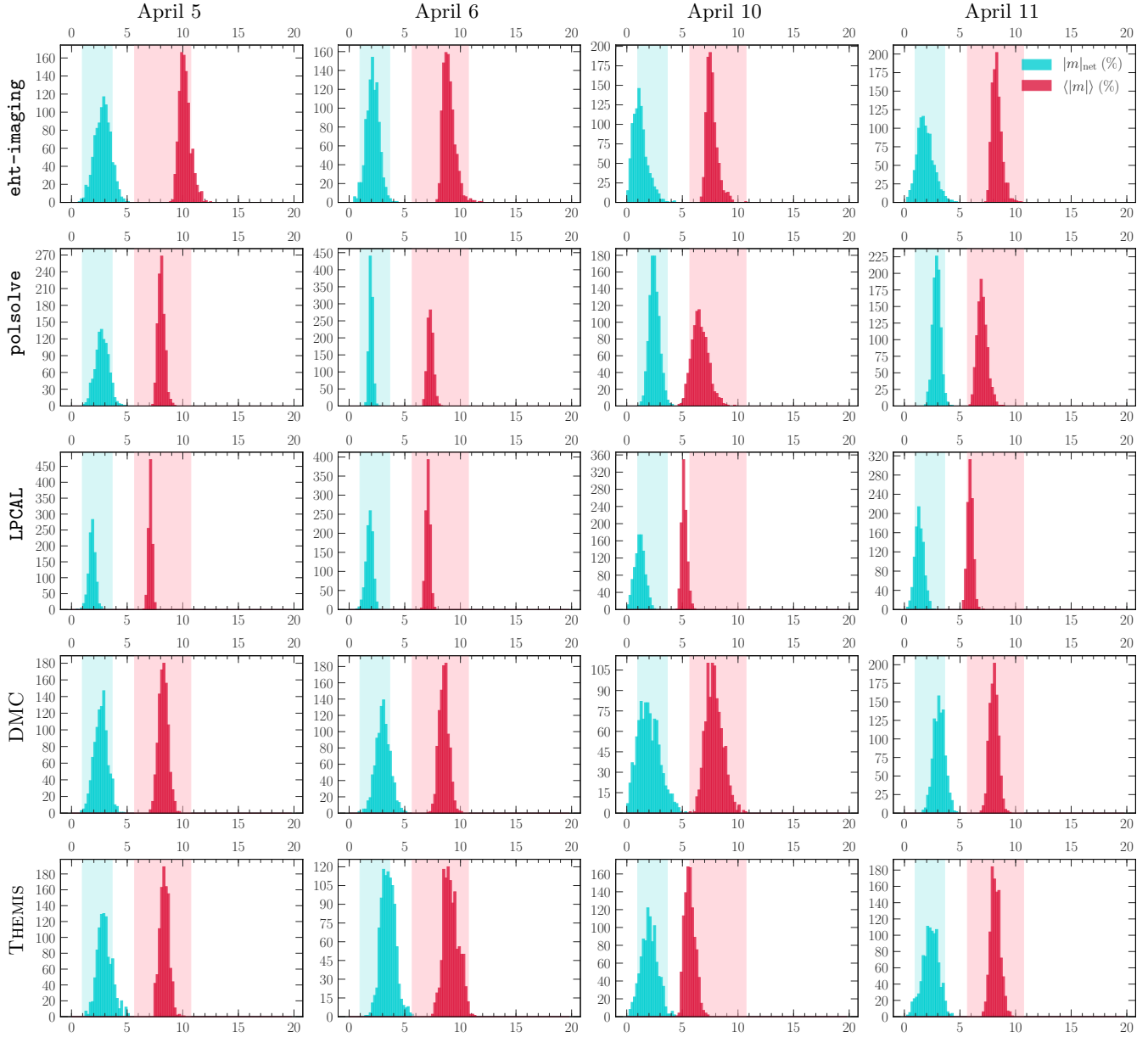
After drawing a given set of random D-terms, we then applied this calibration solution to the data and reconstructed a polarized image using the same procedure and fiducial imaging parameters selected from the parameter survey for each method in Appendix G. Our imaging scripts in this stage differ from those considered in

Appendix G, however, because they do not involve any leakage calibration but only reconstruct the Stokes  $Q$  and  $U$  from the visibilities with the assumed calibration solution applied. That is, we draw a set of random D-terms from distributions reflecting our uncertainty in the recovered D-terms from the earlier parameter survey stage, and then reconstruct an image assuming this D-term calibration is perfect with no further leakage calibration. In contrast, the station amplitude and phase gains are calibrated iteratively in the Stokes  $I$  imaging stage as before.

##### H.2. Distributions of image-averaged parameters

In Figures 25 and 26 we show histograms over each imaging method's sample of 1000 images with different D-term calibration solutions on all four observing days of the four image-integrated quantities used in subsection 5.3. Figure 25 shows histograms of the image net polarization fraction  $|m|_{\text{net}}$  (Equation 12, plotted in red) and the intensity-weighted average polarization fraction at  $20\mu\text{as}$  resolution  $\langle m \rangle$  (Equation 13, plotted in green). Figure 26 shows the amplitude  $|\beta_2|$  (plotted in brown) and phase  $\angle\beta_2$  (plotted in purple) of the  $\beta_2$  coefficient of the azimuthal decomposition defined in Equation 14. Because the observations on April 5 and 11 have the highest-quality  $(u, v)$  coverage and bracket the observed time evolution of the source, we choose to define acceptable ranges for these parameters (the shaded bars in Figures 25, 26, taken from Table 2) using only these two days. In particular, the poor quality of the April 10  $(u, v)$  coverage leads to broader systematic uncertainties between imaging methods (third columns of Figures 25, 26). The distributions on April 5 and 11 are summarized with mean and  $1 - \sigma$  error bars in the main text Figure 9, and discussed in Section 5.3.

Finally, Table 7 presents ranges of the image-integrated Stokes parameters  $I, Q, U$  derived from the



**Figure 25.** Histograms of the net polarization fraction  $|m|_{\text{net}}$  (green: Equation 12) and the image-averaged polarization fraction  $\langle m \rangle$  (red: Equation 13) from each method’s survey over random D-term calibration solutions. From left to right, the four columns show histograms for April 5, 6, 10 and 11. In all panels the shaded bands represent the final parameter ranges reported in this work, incorporating the uncertainty both across D-term realizations and reconstruction methods. These ranges are presented in Table 2. Note that as a consequence of the poor  $(u, v)$  coverage and parallactic angle sampling, the April 10 image reconstructions from all methods show more systematic uncertainty in the derived parameters than on the other days.

surveys over different D-term calibration solutions from each day of observations. The ranges in Table 7 were calculated by taking the minimum mean  $-1\sigma$  and maximum mean  $+1\sigma$  point from the five individual method surveys on each day.

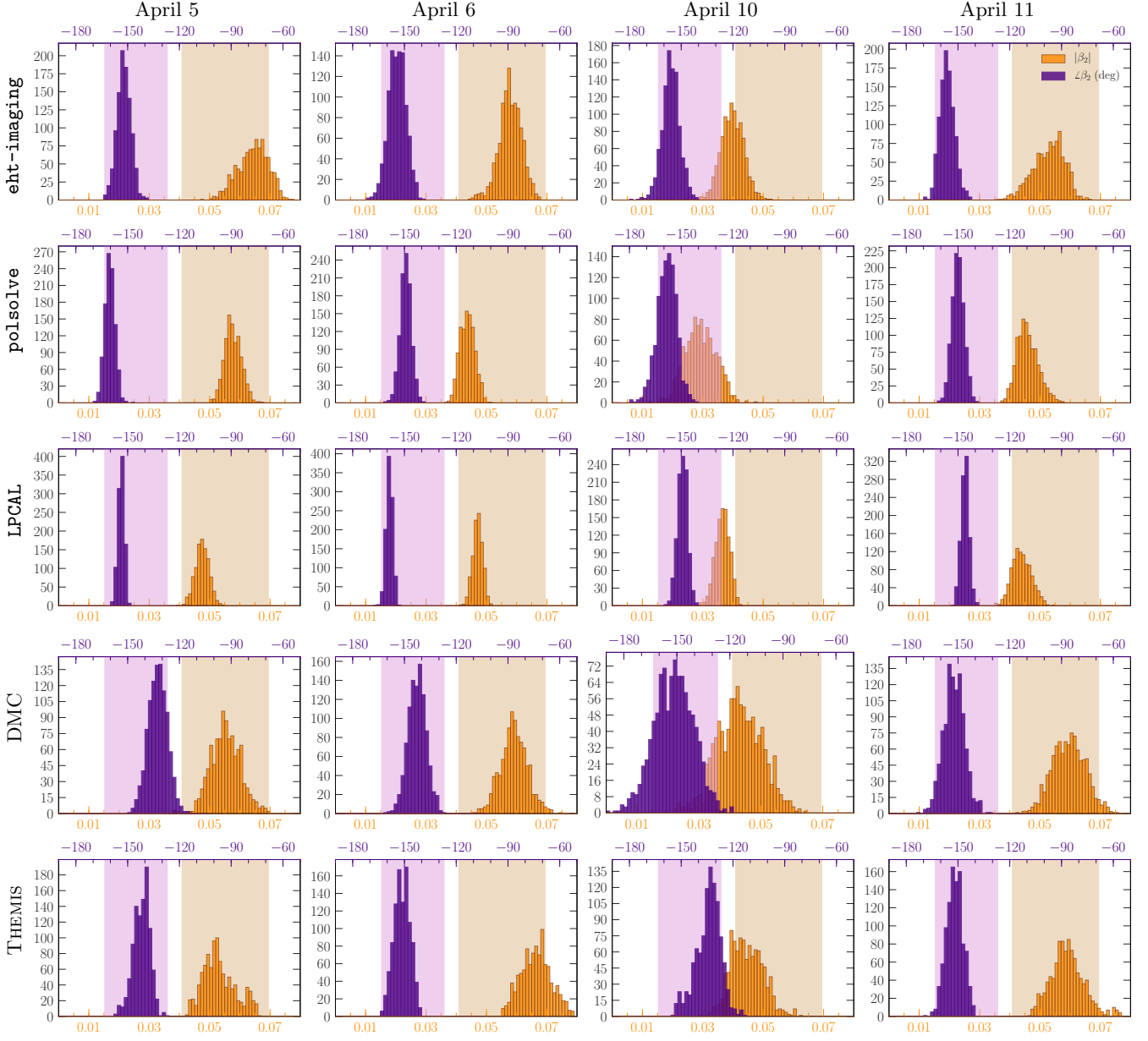
#### I. CONSISTENCY OF LOW AND HIGH BAND RESULTS FOR M87

The results shown in the main text were obtained for the EHT low band data (centered at 227.1 GHz). In

this Appendix, we verify the consistency of these results with the EHT high band data (centered at 229.1 GHz) by repeating several steps of the low band analysis with the same methodology.

##### I.1. Fiducial High Band Images and D-terms

We first compare fiducial D-terms and fiducial polarimetric images derived from the high band data with the low band results reported in the main text (Section 5.1). To produce the high band images, each imaging method



**Figure 26.** Histograms of the amplitude  $|\beta_2|$  (brown: bottom axis) and phase (purple: top axis)  $\angle\beta_2$  of the  $m = 2$  azimuthal mode of the complex polarization brightness distribution (Equation 14) from each method’s survey over random D-term calibration solutions. From left to right, the four columns show histograms for April 5, 6, 10 and 11. In all panels the shaded bands represent the final parameter ranges presented in Table 2. Note that as a consequence of the poor  $(u, v)$  coverage, the April 10 image reconstructions from all methods show more systematic uncertainty in the derived parameters than on the other days.

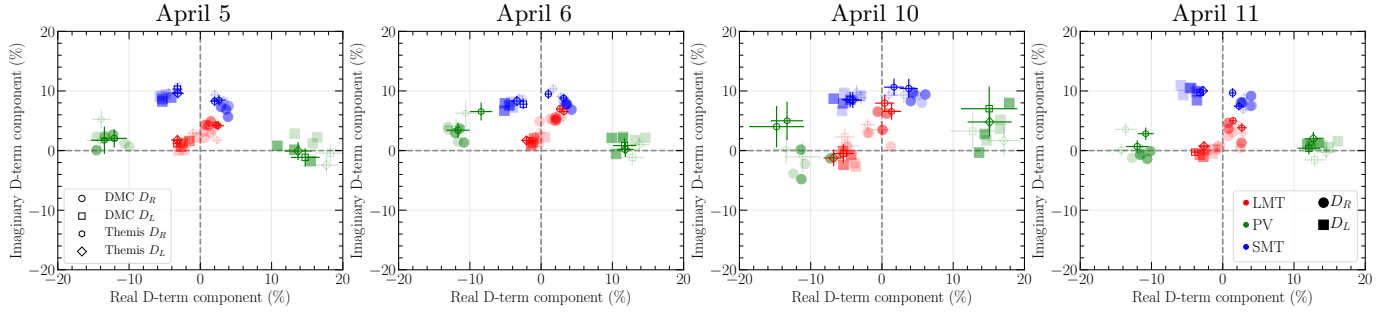
used an identical imaging procedure as for the low band images shown in Figures 6–7 – we did not re-derive parameters specific to each imaging method or repeat the synthetic data surveys described in Section 4.3. This ensures that the methods, while not tuned to high band data, are able to reproduce our most robust results.

Figure 27 shows the low and high band D-terms for LMT, PV, and SMT derived for all five methods. The high band D-terms sit within the systematic scatter among methods in the low band results. Figure 28 com-

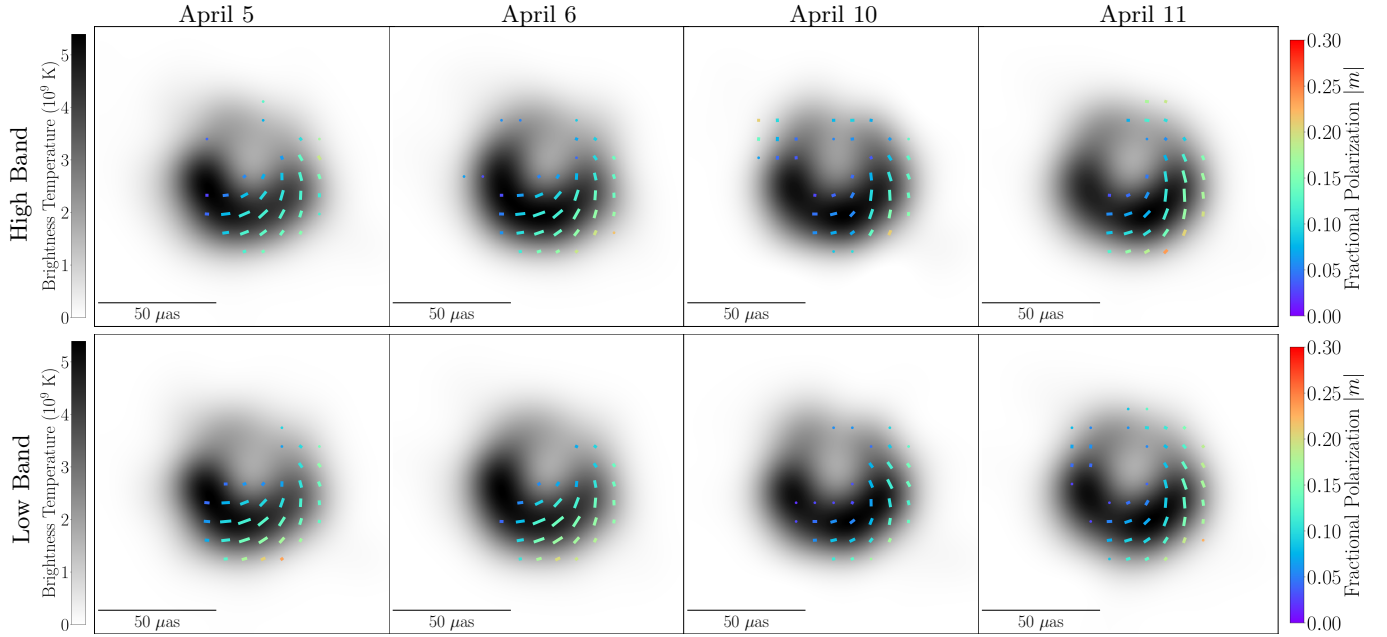
pares the method-averaged high and low band consensus images on all four days. The overall level of linear polarization and azimuthal polarization pattern is consistent between the bands on each day.

### 1.2. Image-averaged quantities

To evaluate the consistency of the image-averaged quantities, we extend the analysis presented in Section 5.3 to the high band data. In particular, we generate a sample of 1000 images from the high band data



**Figure 27.** Fiducial D-terms for LMT, PV, and SMT derived via leakage calibration through `eht-imaging`, `polsolve`, LPCAL polarimetric imaging and DMC/THEMIS posterior exploration of M87 data. The D-terms derived from low band (lighter points) and high band (heavier points) are consistent with one another within the systematic scatter among methods seen in the low band results. All D-terms are displayed in the same manner as in the right panels in Figure 2.



**Figure 28.** Fiducial M87 average images per day produced by averaging results from our five methods (see Figure 6). Method-average images for all four M87 observation days are shown, from left to right. The top and bottom rows show high and low band results, respectively. The images are all displayed with a field of view of  $120 \mu\text{as}$ , and all images were brought to the same nominal resolution by convolution with the circular Gaussian kernel that maximized the cross-correlation of the blurred Stokes  $\mathcal{I}$  image with the consensus Stokes  $\mathcal{I}$  image of Paper IV. Total intensity, polarization fraction, and EVPA are plotted in the same manner as in Figure 6.

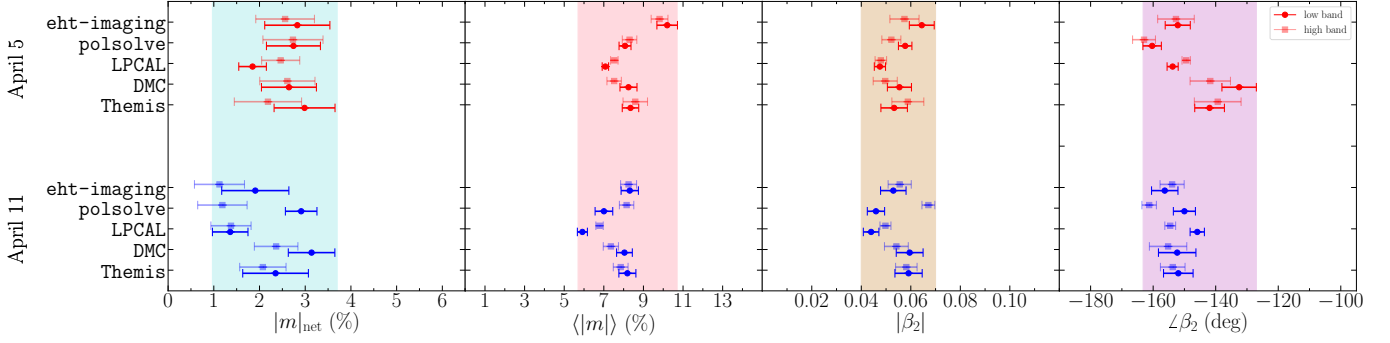
for each method, exploring a range of different D-term calibration solutions (e.g., Figure 24).

Figure 29 compares results for the key image-integrated metrics ( $|m|_{\text{net}}$ ,  $\langle m \rangle$ ,  $\beta_2$ ; see definitions in Section 5.3) derived from such image samples. High band results for a given method are generally consistent within  $1\text{--}2\sigma$  with their low-band counterparts, with the largest offset seen on April 11 for the `polsolve` measurements of  $|m|_{\text{net}}$ ,  $|\beta_2|$  and  $\angle\beta_2$ . The median high band results all fall within the ranges established using the low band images (Table 2), but the high band median- $1\sigma$  points fall outside the established ranges for

the `eht-imaging` and `polsolve`  $|m|_{\text{net}}$  measurements on April 11 and for the `polsolve` measurement of  $|\beta_2|$  on April 5. Because the imaging procedures and results for low band were extensively validated with synthetic data tests, we choose to use the low band results only in defining the parameter ranges in Table 2. Note that  $|m|_{\text{net}}$  in particular can be quite sensitive to the choice of imaging hyperparameters used, and these parameters were not re-derived for the high band data.

Figure 30 compares the image-integrated EVPA measured for high and low band across all four days. For April 6, 10, and 11, the results are consistent for each





**Figure 29.** Comparison of high and low band results for the key quantities used in [Paper VIII](#) on April 5 and 11. The low band results are indicated by circular markers and the high band results are plotted in a lighter color with square markers. The low band results were presented in the main text in [Figure 9](#). The vertical bands indicate the derived parameter ranges from the low-band results presented in [Table 2](#).

Following the same methodology as M87, we generate synthetic data to optimize imaging and calibration parameters for all methods based on J1924–2914 and NRAO 530 low-band coverage. We use the same six ring-like synthetic models as M87 (see [Section 4.3](#)) and add a seventh model constructed with ten Gaussian sources of varying total and polarization intensity, with some polarization structure offset from Stokes  $\mathcal{I}$ . This seventh data set is designed to mimic basic structure seen in the polarimetric images of the two calibrators, for which the final images will be presented in future individual publications (S. Issaoun et al. *in prep.*, S. Jorstad et al. *in prep.*). We generate seven synthetic EHT observations for each source using their best EHT ( $u, v$ ) coverage, April 11 and April 7 for J1924–2914 and NRAO 530 respectively. Parameter surveys are carried out for each method probing the same parameter space as for M87, and fiducial sets were selected with the same selection metrics, see [Appendix G](#).

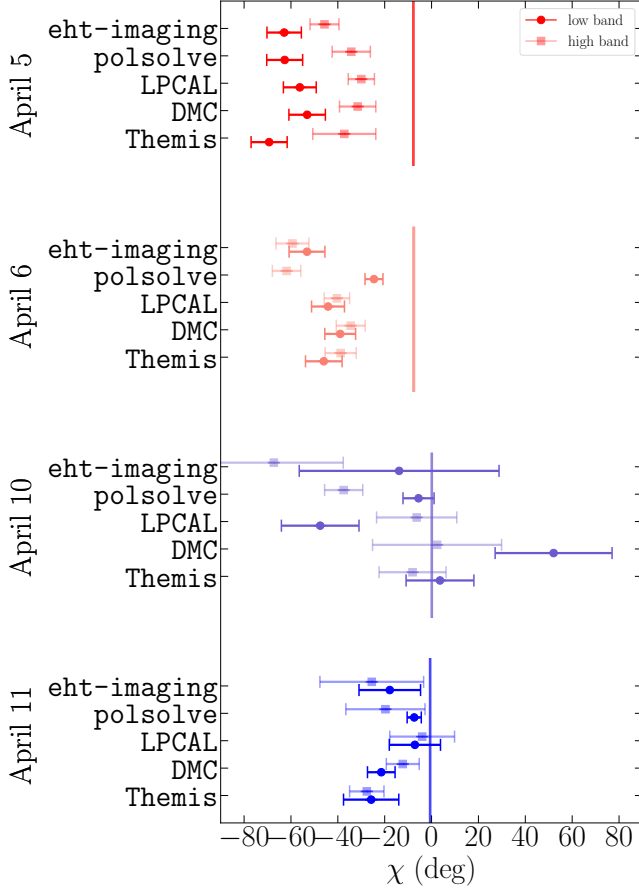
In [Figures 32 and 33](#) we present the set of fiducial images from synthetic reconstructions using J1924–2914 and NRAO 530 best-day low-band coverage respectively. In each panel, the correlations between the ground truth and reconstructed Stokes  $\mathcal{I}$  and linear polarization  $P$  images are provided. Consistent with the results with M87 coverage, the Stokes  $\mathcal{I}$  correlations are high for all models regardless of method and coverage, and  $P$  correlations seem to worsen for models with complex polarization structure or high polarization.

In [Figure 34](#) we compare the recovered leakage D-terms to the ground truth D-terms for the synthetic data sets with coverage from J1914–2914 (top) and NRAO 530 (bottom) and each method. Similarly to the M87 results, PV and SPT have the largest standard deviations for all methods. Their large deviations stem from all methods having difficulty recovering D-terms for models with no strong polarization substructure due to them being isolated stations with only long baselines. Overall, deviations of the D-terms measured via the  $L_1$  norm (and its standard deviation) for the calibrators are

comparable to those for M87 for all methods, but the standard deviation on each D-term estimate is noticeably wider for all stations, indicating that while overall image recovery is similar, the coverage differences between the M87 and the calibrator synthetic data do add uncertainty in the D-term recovery.

Finally, we estimate LMT, SMT and PV D-terms via polarimetric imaging of J1924–2914 and NRAO 530. The polarimetric images of these two calibrators will be presented in forthcoming publications (S. Issaoun et al. *in prep.*, S. Jorstad et al. *in prep.*). Here, in [Figure 35](#), we show that D-terms of LMT, SMT, and PV estimated by imaging the calibrators roughly agree with those of M87. We note that a better agreement is obtained between M87 and J1924–2914 D-terms compared to M87 and NRAO 530. The calibrators have sparser ( $u, v$ ) coverage (fewer scans), narrower field rotation range, and more complex Stokes  $\mathcal{I}$  (extended structure and higher noise level) and polarimetric images compared to M87, which impact D-term estimation quality. Given these additional complexities, we argue that the calibrator D-terms are consistent with those of M87 (the D-term consistency within 2–3% is expected for the calibrators, see also [Appendix K](#)) and that M87 itself is the best source for polarimetric leakage calibration.

Furthermore, while imaging calibrators we found that the quality of Stokes  $\mathcal{I}$  is critical for calibration. Both NRAO 530 and J1924–2914, being blazar sources, have complex jet structure that is not fully recovered with the current EHT coverage, and thus our Stokes  $\mathcal{I}$  reconstructions have larger uncertainties and noise levels than those of M87, due to unconstrained flux density on large scales not sampled by our array configuration. Stokes  $\mathcal{I}$  image assumptions in the polarimetric imaging and calibration methods can affect the results, for example the self-similarity assumption employed for CLEAN reconstructions in our sub-component methods, see [Appendix K](#).



**Figure 30.** EHT net EVPA integrated within  $120 \mu\text{as}$  on all four days for both high and low bands. The low band results are indicated by circular markers and the high band results are plotted in a lighter color with square markers. Vertical lines mark the ALMA-only EVPA measurements from Goddi et al. (2019), measured on arcsecond scales. The low band results for April 5 and 11 were already shown in Figure 10. The image-integrated EVPAs are consistent between high and low band on all days except April 5, where all methods show an offset of  $\sim 20^\circ$ . Note that the image reconstructions and EVPA measurements on April 10 are more uncertain due to the poor  $(u, v)$  coverage.

#### K. VALIDATION OF THE SIMILARITY APPROXIMATION IN CLEAN ALGORITHMS

The D-term estimation using the M87 data with *polsolve* and *LPCAL* reported in Section 4.2 are based on the similarity approximation. The Stokes  $\mathcal{I}$  CLEAN

models are divided into many sub-models to give a high degree of freedom for modelling the source’s linear polarization structures for both software packages. Nevertheless, the complex linear polarization structures of M87 (Figure 6) may not be perfectly modelled with this approximation and this could be a source of uncertainties in the D-term estimation.

We investigate the effect of the similarity approximation by using the instrumental polarization self-calibration mode in *GPCAL* (see Section C.1). We ran *GPCAL* on the M87 data on April 11. The Stokes  $\mathcal{I}$  CLEAN components are divided into 15 sub-models for initial D-term estimation using the similarity approximation. The D-terms of ALMA, APEX, and SMA are fixed to be zero for fitting as they were already calibrated using the intra-site baselines (Section 4.2). The intra-site baselines are flagged since the limited field-of-view of the EHT does not allow us to properly model the source structures observed on the short baselines. Instrumental polarization self-calibration was performed with ten iterations by employing *Difmap* for producing the Stokes Q and U images with CLEAN.

The left panel of Figure 36 compares the D-terms obtained by *GPCAL* with the fiducial D-terms on the same day, i.e., the average of *eht-imaging*, *polsolve*, and *LPCAL* results (Figure 2). Both the results using (i) the similarity approximation only (open squares) and (ii) the similarity approximation followed by ten iterations of instrumental polarization self-calibration (filled circles) are shown. Both of them show a good consistency with the fiducial D-terms with the  $L_1$  norms of  $\approx 1.0 - 1.2\%$ , which is similar to the deviations between values of different pipelines seen in Figure 2. This result indicates that the D-terms obtained by *polsolve* and *LPCAL* using the M87 data are robust against the similarity approximation.

However, this may not be the case for the calibrators. We ran *GPCAL* on the J1924–2914 data on April 11 and NRAO 530 data on April 7. Similar parameters to the M87 data analysis are used. The results are shown in the middle and right panels of Figure 36. The D-terms obtained with instrumental polarization self-calibration are more consistent with the fiducial D-terms than those obtained with the similarity approximation only. The  $L_1$  norms improve from 9.2% to 1.4% and 2.9% to 2.0% for J1924–2914 and NRAO 530, respectively, with the instrumental polarization self-calibration. This result indicates that the linearly polarized structures of the calibrators are complex and cannot be easily modeled with the similarity approximation.

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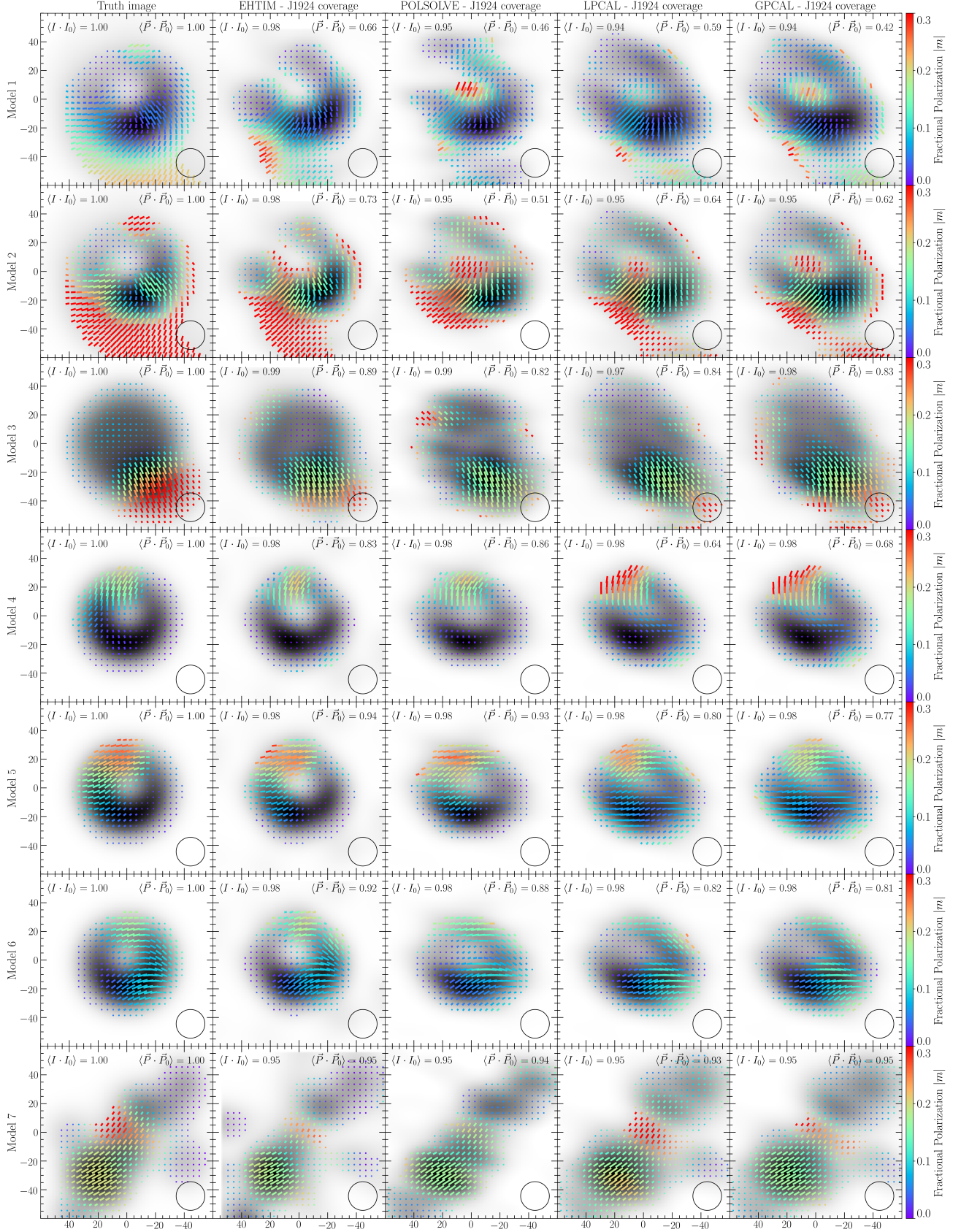
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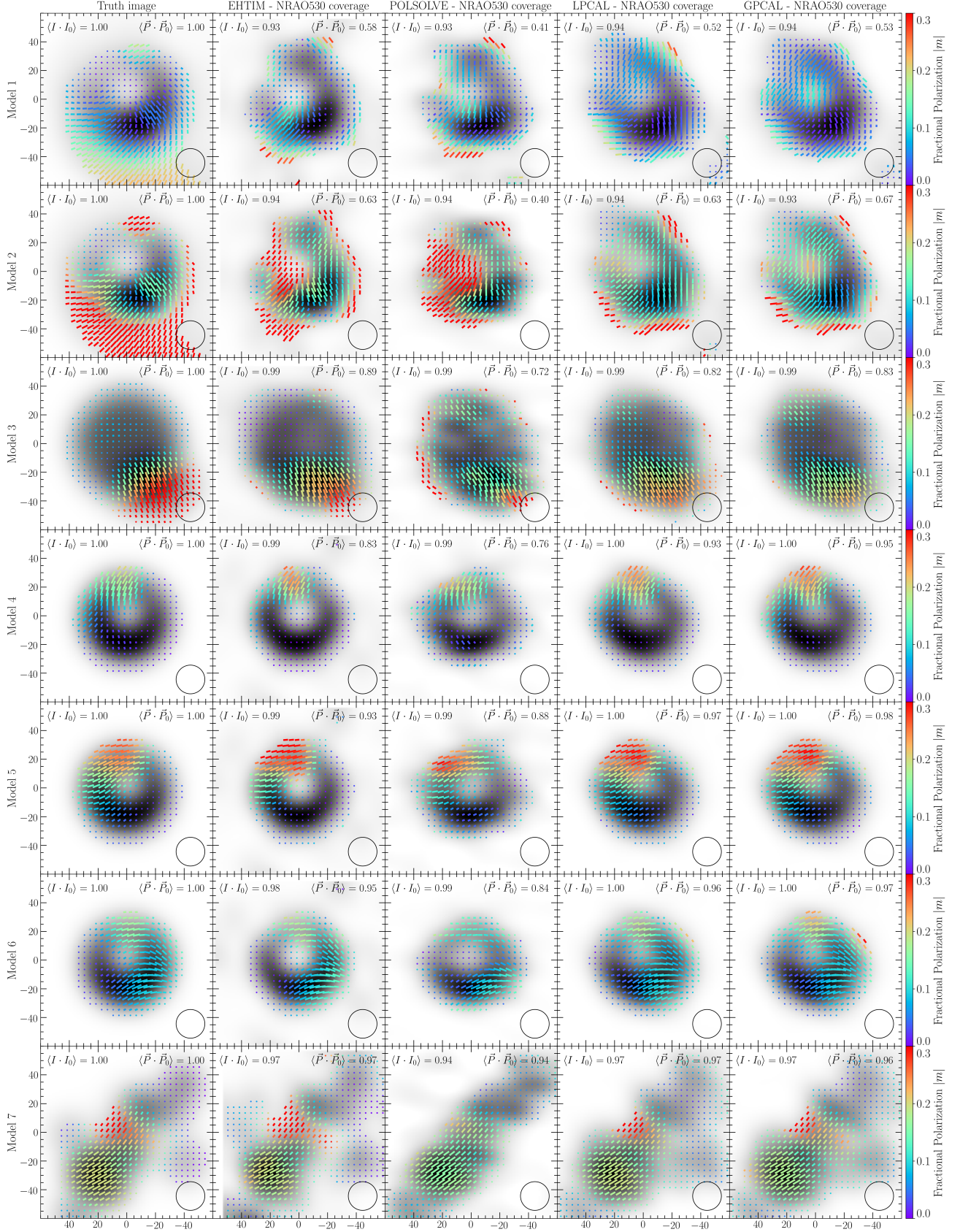
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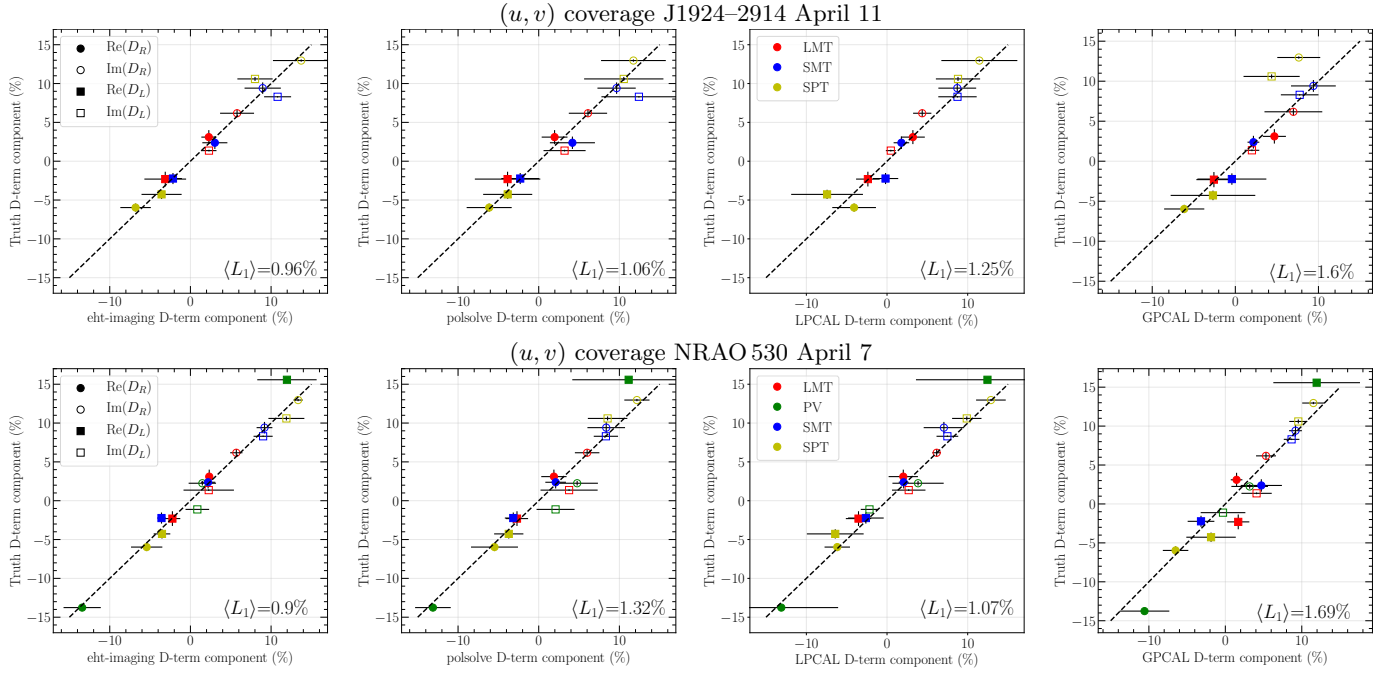


**Figure 32.** Fiducial images from synthetic data model reconstructions using J1924–2014 low band ( $u, v$ ) coverage on April 11. Polarization tick length reflects total polarization, while color reflects fractional polarization from 0 to 0.3. Normalized overlap is calculated against the respective ground truth image, and for the case of total intensity is mean-subtracted.

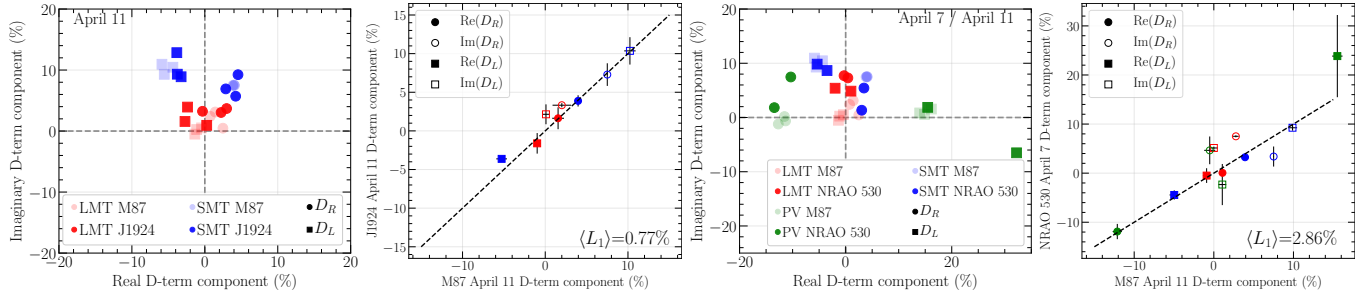




**Figure 33.** Fiducial images from synthetic data model reconstructions using NRAO 530 low band ( $u, v$ ) coverage on April 7. Polarization tick length reflects total polarization, while color reflects fractional polarization from 0 to 0.3. Normalized overlap is calculated against the respective ground truth image, and for the case of total intensity is mean-subtracted.



**Figure 34.** D-terms for LMT, SMT, PV and SPT derived from synthetic datasets. A comparison of estimates to ground truth values is shown per software (`eht-imaging`, `polysolve`, `LPCAL` and `GPCAL` results are shown in first through fourth columns, respectively) and per  $(u, v)$  coverage of the real observations (results for  $(u, v)$  coverage of J1924–2914 on April 11 and the  $(u, v)$  coverage of NRAO 530 on April 7 are shown in the top and bottom panels, respectively). Each data point corresponds to an average and standard deviation for each D-term estimate derived from synthetic data sets 1–7. The norm  $L_1 \equiv |D - D_{\text{Truth}}|$  is averaged over left, right, real, and imaginary components of the D-terms and over all shown EHT stations.



**Figure 35.** Comparison of fiducial D-terms for the telescopes LMT, SMT, and PV estimated from M87 (April 11), J1924–2914 (April 11) and NRAO 530 (April 7) low band data sets using `eht-imaging`, `polysolve`, and `GPCAL` tools. In the first and third panel the M87 D-terms are depicted with lighter symbols while heavier symbols mark the calibrator D-terms. In the correlation plots shown in the second and fourth panels, the D-terms for M87 and J1924–2914/NRAO 530 are averaged over different tools. LMT and SMT D-terms derived from J1924–2914 are found to be highly consistent with those from M87. The D-terms derived from NRAO 530 imaging on average show larger deviation from M87 D-terms; in particular, the PV D-terms estimated by `eht-imaging` show the largest deviation from all other estimates.

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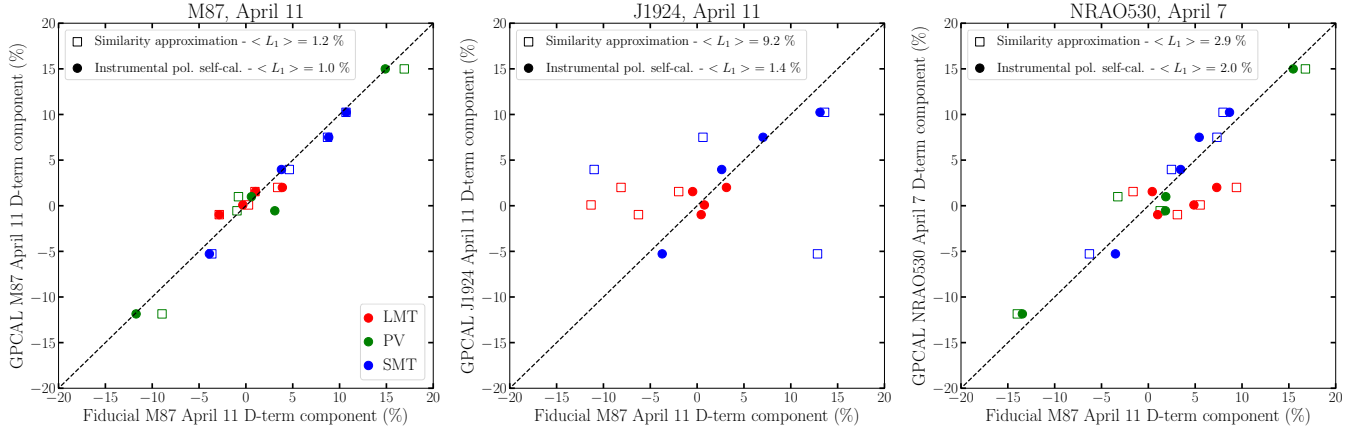
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**Figure 36.** Comparison of D-terms estimated with **GPCAL** with and without using instrumental polarization self-calibration. The average of the D-terms estimated with **eht-imaging**, **polsolve**, and **LPCAL** on the M87 data on April 11 are shown on the  $x$ -axis. The **GPCAL** results with (filled circles) and without (open squares) using instrumental polarization self-calibration are shown on the  $y$ -axis (see text for more details). The left, middle, and right panels show the results of M87 on April 11, J1924–2914 on April 11, and NRAO 530 on April 7, respectively. The  $L_1$  norms do not change much with instrumental polarization self-calibration for M87, while they are significantly improved for the calibrators, especially for J1924–2914. This indicates that the similarity approximation employed by **polsolve** and **LPCAL** for the D-term estimation from M87 (Section 4.2) is reasonable. The calibrators may have complex linear polarization structures and D-term estimation from those sources can be improved with instrumental polarization self-calibration.

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